P2726

#### SEAT No. :

[Total No. of Pages :3

## [5529]-11 M.Sc. PHYSICS

## PHY UT 501 : CLASSICAL MECHANICS (2008 Pattern) (Semester - I)

Time : 3 Hours]

[Max. Marks : 80

Instructions to the candidates:

- 1) Question No. 1 is compulsory and attempt any FOUR questions from the remaining.
- 2) Draw neat diagrams wherever necessary.
- 3) Figures to the right indicate full marks.
- 4) Use of logarithmic table and electronic pocket calculator is allowed.

Q1) Attempt any Four of the following.

- a) A bead slides on a smooth rod which is rotating about one end in a vertical plane with uniform angular velocity ' $\omega$ '. Show that the equation of motion is  $m\ddot{r} = mr\omega^2 mg \sin(\omega t)$  [4]
- b) Prove that generating function  $F = \sum q_k P_k$ , generates identity transformation. [4]
- c) Apply the principle of virtual work to obtain lever equation. [4]
- d) Use Hamilton's equation to prove that the areal velocity is constant in planery motion. [4]
- e) Write down the Hamiltonian for spring mass system and obtain its equation of motion. [4]
- f) Write equations of constraints for [4]
  - i) Simple pendulum with variable length
  - ii) A particle moving on or outside surface of sphere

- Q2) a) Write down the Lagrangian for compound pendulum and obtain its equation of motion.[8]
  - b) Deduce Hamiltonian for simple pendulum and obtain its equation of motion. Also calculate the period of its oscillation. [4]
  - c) State and prove viral theorem. [4]
- Q3) a) A particle describes a circular orbit under the influence of an attractive central force directed towards a point on the circle. Show that the force varies as the inverse fifth power of the distance.[8]
  - b) The transformation equation between two sets of coordinates are  $P = 2(1+q^{\frac{1}{2}}.\cos p)q^{\frac{1}{2}}\sin p$  and  $Q = \log(1+q^{\frac{1}{2}}\cos p)$ .

Show that i) The transformation is canonical

- ii) The generating function of this transformation is  $F = -(e^{\varrho} - 1)^{2} \tan p .$ [8]
- Q4) a) A pendulum of mass 'm'is attached to a block of mass 'M'. The block slides on a horizontal frictionless surface. Find the Lagrangian and equation of motion of the pendulum. For small amplitude oscillation, derive an expression for periodic time.
  - b) What is Focault's pendulum? Obtain its equation of motion. [8]
- **Q5)** a) Prove that  $[F, G]_{q,p} = [F, G]_{Q,P}$  using Poisson's bracket. [8]
  - b) Drive Euler-Lagrange equation and using variational principle show that geodesics of a spherical surface are great circles. [8]

- *Q6)* a) Obtain an expression for Coriolis acceleration for rotating co-ordinate system.
  - b) Write note on artificial satellite.
  - c) Prove the distribution law and multiplication law for Poisson's bracket.[4]

[4]

- (Q7) a) A disc of radius 'a' and mass 'm' rolls down an inclined plane making an angle  $\theta$  with the horizontal. Setup the Lagrangian and find the equation of motion and acceleration of the disc. [8]
  - b) Deduce Hamiltonian for one dimensional harmonic oscillator and obtain its equation of motion. [4]
  - c) Show that the function  $F = -\sum Q_i p_i$  generates the identity transformation. [4]

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P2727

Time : 3Hours/

## [5529]-12 M.Sc. PHYSICS PHYUTN502: Electronics (2008 Pattern) (Semester - I)

[Max. Ma

Instructions to the candidates:

- 1) Question No. 1 is compulsory and attempt any Four questions from the remaining.
- 2) Figures to the right indicate maximum marks.
- 3) Draw neat diagrams wherever necessary.
- 4) Use of logarithrmic table and electronic pocket calculator is allowed.

**Q1)** Attempt <u>any four</u> of the following:

- a) Design a  $\pm$  5V regultted power supply using three pin ICS. [4]
- b) If logic '1'=8V & logic '0'=ov, then determine the following for R-2R type 4 bit DAC.
  - i) Analog output voltage for input 1001
  - ii) Voltage resolution. [4]
- c) Explain with neat circuit diagram, the working of sample and hold circuit.
- d) State any four characteristics/parameters of OPAMP. State their values for ideal OPAMP and IC 741. [4]
- e) Design first order, Butterworth low pass for frequency of 5KHz. Draw its circuit. [4]
- f) What is PLL? Draw its block diagram. Define [4]
  - i) Capture Range ii) Locking Range
- **Q2)** a) Explain with neat circuit diagram, the operation of Astable Multivibrator using IC555.

Design the circuit for  $f_0 = 2$ KHz if c=0.01  $\mu$  f and Vce=+10V with duty cycle of 50% [8]

b) What is Instrumentation Amplifier? Derive the expression for its output voltage using three OPAMP. what are the advantages (at least 2) of an instrumentation amplifier over amplifier? [8]

*P.T.O*.

[4]

[Max. Marks : 80

SEAT No. : [Total No. of Pages :2

- Q3) a) Draw the a function diagram of 4 bit shift register using IC 7495. Explain its working with night and left shift operation for a data 1010 with necessary timing diagram/wave form.
  - b) What is meant by precision Rectifier? Explain with neat circuit diagram, the working of a full-wave precision rectifier using OPAMP. Draw its input and output waveforms. [8]
- Q4) a) Draw a block diagram of IC723 voltage regulator. Design a voltage regulator for 5V output with current of 0.1A, using IC723 voltage regulator. Draw its circuit diagram.
  - b) Draw a combinational logic circuit to implement following expression.  $Y = \sum_{m} (0, 2, 4, 5, 8, 10, 12, 15)$ How it can implemented using multiplexer?

[8]

[16]

Q5) a) With neat block diagram, state the function of each block of function generator IC 8038. Design this function generator for output frequency of 10 KHz.

- b) What is VCO? Explain its working with neat block diagram of IC 566.
  Design VCO using IC 566 to generate a wave form ferquency range from 2KHz to 10 KHz (Given Vcc = 10v.) [8]
- Q6) a) What is decade counter? State its applications. How IC7490 decade counter can be used to construct MOD.5 counter? [8]
  - b) Design a notch filter using twin -T network, for  $f_n = 50$ Hz and Q=5. Determine its  $f_{\mu}f_{\mu}$  and bandwidth. Draw its frequency response curve.[8]
- Q7) Write short notes on any four of the following:
  - a) Monostable multivibrator using IC 74121.
  - b) Frequency spectrum –MW,SW,FM,LHF and its application.
  - c) Counter type ADC.
  - d) Karnaugh map and its use in BCD to gray code conversion.
  - e) Switching mode power supply.
  - f) Binary Weighted Resistor type DAC (4bit)

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[5529]-12

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#### **P2728**

## [5529]-13 M.Sc. PHYSICS

## **PHY UTN-503 : Mathematical Methods in Physics** (2008 Old Pattern) (Semester-I)

Time : 3 Hours]

Instructions to the candidates:

- Question No. 1 is compulsory. Attempt <u>ANY FOUR</u> questions from the remaining. 1)
- 2) Draw neat diagrams wherever necessary.
- 3) Figures to the right indicate full marks.
- Use of logarithmic table and calculator is allowed. 4)

**Q1)** Attempt <u>ANY FOUR</u> of the following:

Let  $V = R^3$ . Determine whether W is a subspace of V, where: a) [4]

5

W = { $(a,b,c): a^2 + b^2 + c^2 \le 0$ }

- Define Basis and dimension of a vector space. Is dimension of a particular b) vector space unique? Explain. [4]
- State and explain the Dirichlet conditions. [4] c)
- Determine the residue of d)

$$\frac{ze^{zt}}{\left(z-3\right)^2} \text{ at } z=3$$

Prove that: e)

$$J_{n+1}(x) = \frac{2n}{x} J_n(x) - J_{n-1}(x)$$

Obtain the first two Hermite's polynomials. f) [4]

*P.T.O.* 

[Total No. of Pages : 3

[4]

[4]

[Max. Marks : 80

**SEAT No. :** 

(Q2) a) Let V be the vector space of polynomials with inner product given by

$$\left\langle f,g\right\rangle = \int_{0}^{1} f(t) g(t) dt \text{ . Let } f(t) = t + 2 \text{ and } g(t) = t^{2} - 2t - 3. \text{ Find } \left\langle f,g\right\rangle$$
  
and  $\|f\|$ . [8]

b) State and prove the orthogonality property of Legendre polynomials.[8]

- b) Using the Rodrigue's formula for Laguerre's polynomials obtain the first three Laguerre polynomials. [8]
- Q4) a) State Residue theorem. Explain how the Cauchy's theorem and integral formulas are special cases of residue theorem. [8]
  - b) Determine the first three Legendre polynomials  $P_0(x)$ ,  $P_1(x)$  and  $P_2(x)$ . [8]

**Q5)** a) Find 
$$L^{-1}\left\{\frac{3s+1}{(s-1)(s^2+1)}\right\}$$
. [8]

b) Find eigenvalues and eigenvectors of matrix A =  $\begin{pmatrix} 1 & -3 & 3 \\ 3 & -5 & 3 \\ 6 & -6 & 4 \end{pmatrix}$ . [8]

*Q6*) a) Find the Fourier transform of:

$$f(x) = 1 |x| < a$$
  
$$f(x) = 0 |x| > a$$

b) Let  $A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}$  and let T be the linear operator on  $R^2$  defined by T(V) = AV (Where V is written as a column vector). Find the matrix of T

i) 
$$\{e_1 = (1,0), e_2 = (0,1)\}$$
, i.e. usual basis;

ii) 
$$\{f_1 = (1,3), f_2 = (2,5)\}.$$

**Q7)** a) State and prove Parseval's identity for Fourier series. [4]

b) Discuss whether or not 
$$\mathbb{R}^3$$
 is a subspace of  $\mathbb{R}^4$ . [4]

d) Let f(t) be continuous and have a piecewise continuous derivative f'(t) in every finite interval  $0 \le t \le T$ . Suppose also that f(t) is of exponential order for t > T. Then prove that: [4]

$$L\{f'(t)\} = sL\{f(t)\} - f(0).$$

$$\rightarrow$$
  $\rightarrow$   $\rightarrow$ 

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[8]

#### P2729

#### [5529]-14

#### M.Sc.

#### PHYSICS

## PHY UTN-504 : Quantum Mechanics - I (2008 Pattern) (Semester-I)

Time : 3 Hours]

Instructions to the candidates:

- 1) Question 1 is compulsory, Attempt four from the remaining.
- 2) Draw neat diagrams wherever necessary.
- 3) Figures to the right indicate full marks.
- 4) Use of calculators allowed.
- Q1) Attempt any four of the following:
  - a) Prove that  $[x^n, p] = i\hbar nx^{n-1}$ , where x and p are position and momentum operators.
  - b) Prove that  $[L_x, L_y] = i\hbar L_z$  and  $[L+, L-] = 2\hbar L_z$ .
  - c) Show that the Pauli spin matrices satisfy the commutation relation  $\left[\sigma^2, \sigma_z\right] = 0$ .
  - d) Explain Hilbert space in detail.
  - e) Using uncertainty principle estimate ground state energy of harmonic oscillator.
  - f) For  $j = \frac{1}{2}$ , obtain the matrix Jx.

[Total No. of Pages : 3

**SEAT No. :** 

[16]

[Max. Marks: 80

- (Q2) a) Establish Schrödinger equation for an infinite deep potential well and obtain eigen functions and eigen values.[8]
  - b) Explain completeness and closure property of eigen functions. [8]
- **Q3)** a) Explain Heisenber picture. Show that [8]

$$i\hbar \frac{dA}{dt} = [A,H] + i\hbar \frac{\partial A}{\partial t}$$

- b) State and explain postulates of quantum mechanics. [8]
- Q4) a) Using ladder operators obtain energy eigen values of one dimensional harmonis oscillator.
  - b) Explain Hermitian operator. Show that eigen functions corresponding to distinct eigen values of Hermitian operator are orthogonal. [8]
- **Q5)** a) Define norm and scalar product in Hilbert space for arbitrary vectors  $|\psi\rangle$  and  $|x\rangle$ . Prove that [8]

i) 
$$\langle a | \hat{A} | a \rangle = a' \delta a a'$$

ii) if  $\langle \psi | \psi \rangle = 1$  and U is unitary prove that  $\langle U \psi | U \psi \rangle = 1$ .

b) Show that momentum operator is Hermitian [8]

- **Q6)** a) Using as a basis of eigen vectors  $|jm\rangle$  of  $J^2$  and  $J_z$ , obtain matrix representation of the angular momentum operators  $J_x$ ,  $J_y$  and  $J_z$ . [8]
  - b) Define projection operator. Show that the sum of all projection operators leaves any state vector  $|\psi\rangle$  unchanged. [8]
- **Q7)** a) Show that  $(x p_x)^2 \neq x^2 p_x^2$ , where x and  $p_x$  are position and momentum operators respectively. [4]
  - b) If A is anti-Hermitian, show that  $e^{A}$  is unitary. [4]
  - c) Show that Hermitian operator retains its Hermitian characteristics under unitary transformation. [4]
  - d) If  $\psi_1$  and  $\psi_2$  are eigen functions of an operator then prove that their linear combination is also a eigen function of the same operator. [4]

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#### [5529]-21 M.Sc. - I PHYSICS

## PHYUTN-601 : Electrodynamics (2008 Pattern) (Semester - II)

Time : 3 Hours]

Instructions to the candidates:

- 1) Q.No. 1 is compulsory and solve any four questions from the remaining.
- 2) Draw neat labelled diagrams wherever necessary.
- 3) Figures to the right side indicate full marks.
- 4) Use of logarithmic tables and calculator is allowed.

**Q1)** Attempt any four of the following :

- a) Write Maxwell's equations in differential and integral forms. [4]
- b) Explain the term 'momentum space' with the help of suitable example.[4]
- c) Calculate the frequency at which the skin-depth in sea water is 1 meter.

Given : 
$$\mu_0 = \mu = 4\pi \times 10^{-7} \frac{\text{Wb}}{\text{A}-\text{m}} \text{ and } \sigma = 4.3 \frac{\text{mho}}{\text{m}}.$$
 [4]

- d) Show that the ratio of electrostatic and magnetic energy densities is equal to unity. [4]
- e) Determine the velocity at which the mass of a particle is double its rest mass. Given :  $C = 3 \times 10^8$  m/s. [4]
- f) Explain Minkowski's space-time diagram. [4]
- Q2) a) Derive an expression for potential at a distant point using multipole expansion for a localized charge distribution in free space.[8]
  - b) Describe Michelson-Morley experiment wth a suitable diagram. Hence derive the formula for fringe shift. [8]
- Q3) a) Using the concept of e.m. energy, show that power transferred to the e.m. field through the motion of charge in volume V is given by : [8]

$$-\int_{V} \left(\vec{j} \cdot \vec{E}\right) dV = \frac{d}{dt} \int_{V} \frac{1}{2} \left(\vec{E} \cdot \vec{D} + \vec{B} \cdot \vec{H}\right) dV + \int_{CS} \left(\vec{E} \times \vec{H}\right) dS$$

b) State and prove Poynting's theorem.

[8]

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[Total No. of Pages : 2

[Max. Marks : 80

SEAT No. :

- Q4) a) With the help of suitable diagram explain the magnetic interaction between two current loops. [8]
  - b) Derive the Lorentz relativistic transformation equations. [8]
- **Q5)** a) The magnetic field intensity  $\vec{B}$  at a point is given by : [8]

$$\vec{\mathrm{B}} = \left(\frac{\mu_0}{4\pi}\right) \int \frac{\vec{j} \times \vec{r}}{r^3} dr$$
, show that  $\vec{\nabla} \times \vec{\mathrm{B}} = \mu_0 j$ .

- b) Explain the term electromagnetic field tensor. Hence obtain an expression for e.m. field tensor  $F_{\mu\nu}$ . [8]
- **Q6)** a) Calculate the magnitude of Poynting's vector at the surface of the sun. Given : Power radiated by sun is equal to  $3.8 \times 10^{26}$  Watt and radius of the sun is equal to  $7 \times 10^8$  m. [8]
  - b) Prove that the space interval  $x^2 + y^2 + z^2$  is not invariant under Lorentz transformations, while combined space-time interval  $x^2 + y^2 + z^2 c^2t^2$  is Lorentz invariant. [8]

- b) Find the velocity at which the mass of the particle is double its rest mass. Given :  $C = 3 \times 10^8$  m/s. [4]
- c) Explain the term 'Four Vector Potential'. [4]
- d) Find the wave impedance of an e.m. wave travelling through free space.

Given: 
$$\mu_0 = 4\pi \times 10^{-7} \frac{\text{Wb}}{\text{A} - \text{m}} \& \in_0 = 8.85 \times 10^{12} \frac{\text{C}^2}{\text{N-m}^2}.$$
 [4]

#### P2732

## [5529]-23 M.Sc.

#### PHYSICS

## PHY UTN-603 : Statistical Mechanics in Physics (2008 Pattern) (Semester-II) (Old)

*Time : 3 Hours]* 

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Instructions to the candidates:

- 1) Question No. 1 is compulsory, attempt any four questions from the remaining questions.
- 2) Draw neat diagrams wherever necessary.
- 3) Figures to the right indicate full marks.
- 4) Use of logarithmic tables and electronic pocket calculators is allowed.

#### Constants:-

- 1) Boltzman's constant  $k_{B} = 1.38 \times 10^{-23}$  Joule/°k.
- 2) Plank's constant  $h = 6.625 \times 10^{-34}$  Joule sec.
- 3) Avogadro's number  $N = 6.023 \times 10^{23}$  mole<sup>-1</sup>.
- 4) Mass of electron  $me = 9.1 \times 10^{-31} kg$ .
- 5) Velocity of light  $c = 3 \times 10^8$  m/s.

**Q1)** Attempt any four of the following:

- a) Explain macrostate and microstate of a system. [4]
- b) Obtain the mean energy of femions at absoute zero. [4]
- c) The energy of particle moving in a rigid cubical box is specified by the equation. [4]

$$n_x^2 + n_y^2 + n_z^2 = \frac{2mc^2 E}{n^2 h^2} = 14$$

Determine the number of microstates accessible to the particle.

- d) What is mechanical interaction? [4]
- e) Compare the basic postmasters of B.E. and F.D. Statistics. [4]

[Max. Marks : 80

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**Q2)** a) State and prove equipartition theorem.

- b) Show that photons the mean pressure  $\langle P \rangle$  is related to its total energy E is given by the relation  $\langle P \rangle = \frac{1}{3} \frac{\langle E \rangle}{V}$ . [8]
- **Q3)** a) State and prove Lianville's theorem in classical statistics. [8]
  - b) For grand cannonical ensemble, show that probability of finding the system in a particular microstate "r" having Energy  $E_r$  and number of particles  $N_r$  is given by  $P_r = \frac{e^{-\beta E_r \alpha N_r}}{\sum_r e^{-\beta E_r \alpha N_r}}$ . [8]
- **Q4)** a) Calculate the mean values  $\overline{E}$  and  $(\Delta E)^2$  for canonical energy line in terms of partition function. [8]
  - b) On the basis of canonical distribution, obtain the law of atmosphere  $p(z) = p(0)e^{-mg^2/kT}$ . [8]
- Q5) a) Use canonical distribution to discuss the behavior of paramagnetic substance placed in an external magnetic field. Hence obtain magnetic susceptibility of para-magnetic substance.
  [8]
  - b) State the expression for quantum distribution function  $\overline{n_s}$  and obtain BE distribution in the form  $\overline{n_s} = \frac{1}{e^{\beta(eS-\mu)-1}}$  where  $\mu$  is chemical potential. [8]

**Q6)** a) Obtain Maxwell's velocity distribution and hence show that the radio of root mean square velocity  $v_{\text{max}}$  to mean velocity  $\overline{v}$  to the most probable

velocity 
$$\overline{v}$$
 is given by  $v_{\text{max}} = \overline{v} : \overline{v} \equiv \sqrt{3} : \sqrt{\frac{8}{\pi}} : \sqrt{2}$ . [8]

- b) In case of Bose-Einstein condensation for  $T < T_B$  prove that  $N = N_0 + N \left(\frac{T}{T_B}\right)^{3/2} \text{ where.}$ [8]
  - N = total Number of particles and
  - $N_0 =$  total number of particles in ground state.
- (Q7) a) Show that for diatomic molecule when  $T \ll \theta_v$  where  $\theta_v$  is the vibrational characteristics temperature  $(Cv)_{vib} = N_k \left(\frac{\theta v}{T}\right)^2 e^{-\theta v/T}$ . [8]
  - b) Derive the expression of Stefan's law for Black Body radiation. [8]

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P2733

## [5529]-24 M.Sc.

#### WI.SC.

#### PHYSICS

### PHYUTN-604 : Quantum Mechanics - II (2008 Pattern) (Semester-II)

Time : 3 Hours]

Instructions to the candidates:

- 1) Question 1 is compulsory. Solve any four from remaining.
- 2) Draw neat diagrams wherever necessary.
- 3) Figures to the right indicate full marks.
- 4) Use of log-tables and calculators allowed.

**Q1)** Attempt any four of the following:

- a) Define exchange operator. Show that eigen values of exchange operator are ±1. [4]
- b) Discuss the selection rules for dipole transitions. [4]
- c) Show that there is no Stark effect in the ground state of hydrogen atom.[4]
- d) The harmonic oscillator is perturbed by H<sup>1</sup>=bx<sup>3</sup>. Obtain first order correction in energy for ground state. [4]
- e) Explain Laboratory and Centre of mass frames of reference. [4]
- f) Find the energy levels and eigen functions of Hamiltonian

 $H = \begin{bmatrix} 1 + \varepsilon & \varepsilon \\ \varepsilon & 1 + \varepsilon \end{bmatrix}$ . Where  $\varepsilon << 1$ , corrected upto first order in  $\varepsilon$  using perturbation theory. [4]

- Q2) a) Starting from perturbation state, obtain first order corrections in energy in case of stationary degenerate states. [8]
  - b) Write down connection formulae in WKB approximation. Hence obtain Bohr-Sommerfield quantization rule. [8]

[Max. Marks : 80

*P.T.O.* 

#### SEAT No. :

[Total No. of Pages : 2

- Q3) a) Using partial wave analysis, obtain the expression for scattering amplitudes and total scattering cross-section.
  - b) Obtain Slater determinant for system of N electrons. [8]
- Q4) a) Show that the Born scattering amplitude is proportional to the spatial Fourier transform of the scattering potential with respect to the momentum transfer.
  - b) What is Harmonic perturbation? Calculate transition probability per unit radiation of intensity of a harmonic perturbation. [8]
- **Q5)** a) Apply variational method to estimate the ground state of a hydrogen atom (Use trial wave function  $N(r) = \overline{e}^{\alpha r}$ , where  $\alpha$  is variational parameters). [8]
  - b) Develop time-dependent perturbation theory to obtain first order correction to the amplitude  $a_m^{(1)}(t)$ . [8]
- *Q6)* a) Use WKB approximation to illustrate the of alpha-decay from radioactive nucleus.[8]
  - b) What are identical particles? Obtain symmetric and anti-symmetric wave functions for a system of two electrons. [8]
- (Q7) a) State the conditions of validity of Born approximation for scattering.[4]
  - b) Show that variational method gives an upper bound to the ground state energy. [4]
  - c) Discuss concept of symmetry in quantum mechanics. [4]
  - d) State the condition of validity of WKB approximation. [4]



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#### SEAT No. : [Total

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## [5529]-31 M.Sc. PHYSICS

## PHYUTN-701 : Solid State Physics (2008 Pattern) (Semester - III)

Time : 3 Hours]

Instructions to the candidates:

- 1) Question No. 1 is compulsory and solve any four questions from the remaining.
- 2) Figures to the right indicate full marks.
- 3) Draw neat labelled diagrams wherever necessary.
- 4) Use of logarithmic table and pocket calculator is allowed.

#### Given :

Mass of electron =  $9.1 \times 10^{-31}$  Kg Charge of electron =  $1.6 \times 10^{-19}$  C Plank's constant =  $6.626 \times 10^{-34}$  J-s Boltzmann constant =  $1.38 \times 10^{-23}$  J/k Avogadro's number =  $6.023 \times 10^{26}$  / Kmol Bohr magneton =  $9.27 \times 10^{-24}$  A-m<sup>2</sup> Permeability of free space =  $4\pi \times 10^{-7}$  Henry/m Permittivity of free space =  $8.85 \times 10^{-12}$  C<sup>2</sup>/N-m<sup>2</sup>

Q1) Attempt any four of the following :

- a) Show that for Kronig Penny potential with p<<1 the energy of the lowest energy band at k = 0 is  $E = \hbar^2 p / ma^2$ .
- b) A paramagnetic material is subjected to a homogeneous field of 10<sup>6</sup> A/m at 37°C. Calculate the average magnetic moment along the field direction per spin in Bohr magneton.
- c) Calculate the critical current density which can flow through a long thin superconducting wire of Al of diameter  $10^{-3}$  m. The critical magnetic field for Al is  $7.9 \times 10^{3}$  A/m.
- d) Estimate the fraction of electrons excited above Fermi level at 27°C for sodium and copper if Fermi level values are  $E_F = 3.1$  eV for sodium and  $E_F = 7$  eV for copper.

[Max. Marks : 80

[16]

- e) A circular loop of conductor having a diameter of 0.5 m carries a current of  $10^5 \,\mu$ A. Calculate the values of magnetic dipole moment. The loop is placed in a magnetic field having a uniform flux density of 0.05 Wb/m<sup>2</sup> with its axis inclined at 60° to the direction of field. Hence calculate the torque experienced by the current loop.
- f) The relative permittivity of argon at 0°C and one atmosphere is 1.000435. Calculate the polarizibility of the atom.
- Q2) a) Derive London's equation for super conducting state and obtain an expression for London's penetration depth.[8]
  - b) Discuss the origin of diamagnetism in a free atom. Obtain Langevin's diamagnetism equation for the diamagnetic susceptibility. [8]
- Q3) a) Describe the motion of electron in one dimensional periodic potential. Explain the concept of effective mass m\*. Draw E-K, V-K and m\*-K diagrams.
  - b) Define polarizibility in dielectrics. Explain different types of polarizibilities. Represent total polarizibility as a function of frequency graphically. **[8]**
- Q4) a) Give an account of Weiss theory of ferro-magnetism and show from the plot of Langevin's function, spontaneous magnetization exists below the Curie temperature and vanishes above the Curie temperature.[8]
  - b) Define dielectric function of the free electron gas. Derive the expression for plasma frequency. [8]
- **Q5)** a) For antiferromagnetic substances, prove the following relation for Neel temperature

$$\frac{\mathrm{T_{N}}}{\theta} \!=\! \frac{\lambda_{ij} - \lambda_{ii}}{\lambda_{ij} + \lambda_{ii}}$$

Symbols have usual meaning.

b) State Bloch theorem. Prove it for the function  $\phi_K$  for a general potential at value K. [8]

[5529]-31

[8]

- **Q6)** a) Explain the assumptions of BCS theory of superconductivity. [8]
  - Explain the concept of Bloch wall with reference to magnetism.[4] b) i)
    - ii) What are the assumptions of nearly free electron model. [4]
- Write expression for F-D statistics and explain how it changes with **Q**7) a) temperature. [4]
  - A magnetic material has a magnetization of 3300 A/m and magnetic flux b) density of  $4.4 \times 10^{-3}$ T. Calculate the magnetizing force. [4]
  - Explain flux quantization in super conducting ring. c) [4]
  - Draw diagrams for Fermi surfaces in first, second and third Brillouin d) zones. [4]