

Name of Course	: CBCS (LOCF) Generic Elective- Mathematics
Unique Paper Code	: 32355101
Name of Paper	: GE-1 Calculus
Semester	: I
Duration	: 3 hours
Maximum Marks	: 75 Marks

Attempt any four questions. All questions carry equal marks.

1. Find all vertical and horizontal asymptotes of the graph of the function $f(x) = \frac{4x+5}{8-x}$.

Also, find the interval in which $f(x)$ is,

- (i) increasing and decreasing
- (ii) concave up and concave down.

Determine points of inflection, if any and give a rough sketch of the graph.

2. Find the indeterminate form and evaluate the following limits using L'Hôpital's rule

- (i) $\lim_{x \rightarrow 0} \left(\frac{1}{\sin 3x} - \frac{1}{3x} \right)$
- (ii) $\lim_{x \rightarrow +\infty} \left(\frac{\log x}{x^7} \right)$
- (iii) $\lim_{x \rightarrow +\infty} (x)^{1/2x}$.

3. Find the volume of the solid generated when the region enclosed between $y = \sqrt{x}$, $x = 1$, $x = 4$ and the x -axis is revolved about the y -axis using washer method and cylindrical shell method.

4. Describe the graph of the following

- (i) $x^2 + 8y - 6x - 23 = 0$
- (ii) $y^2 - x^2 - 6y - 4x + 4 = 0$.

Also label the vertices, foci, directrix or asymptotes in each case.

5. Determine the largest region on which the following functions are continuous. Justify your answer.

(i)
$$f(x, y) = \begin{cases} \frac{xy^2}{x^2+y^4}, & (x, y) \neq (0, 0) \\ 0, & (x, y) = (0, 0) \end{cases}$$

(ii)
$$g(x, y) = \frac{\sin x + \cos y}{2 + \sin x}, \quad (x, y) \in \mathbb{R}^2.$$

6. Locate all relative maxima, relative minima and saddle points, if any of the following functions.

(i) $f(x, y) = 3x^2 + 12x + 8y^3 - 12y^2 + 38$

(ii) $g(x, y) = \frac{1}{x} + \frac{1}{y} + xy + 13.$