**6MA SLM-T** 



# New York State Testing Program

# 2017 Common Core

# **Mathematics Test**



# **Scoring Leader Materials**

**Training Set** 

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#### **Grade 6 Mathematics Reference Sheet**

#### CONVERSIONS

1 inch = 2.54 centimeters 1 kilometer = 0.62 mile 1 cup = 8 fluid ounces 1 meter = 39.37 inches 1 pound = 16 ounces1 pint = 2 cups 1 mile = 5,280 feet 1 pound = 0.454 kilogram 1 quart = 2 pints 1 mile = 1,760 yards1 kilogram = 2.2 pounds 1 gallon = 4 quarts1 mile = 1.609 kilometers 1 ton = 2,000 pounds1 gallon = 3.785 liters 1 liter = 0.264 gallon 1 liter = 1,000 cubic centimeters

RMULAS	
friangle	$A = \frac{1}{2}bh$
Right Rectangular Prism	V = Bh  or  V = Iwh

#### 2-Point Holistic Rubric

2 Point	<ul> <li>A two-point response includes the correct solution to the question and demonstrates a thorough understanding of the mathematical concepts and/or procedures in the task.</li> <li>This response <ul> <li>indicates that the student has completed the task correctly, using mathematically sound procedures</li> <li>contains sufficient work to demonstrate a thorough understanding of the mathematical concepts and/or procedures</li> <li>may contain inconsequential errors that do not detract from the correct solution and the demonstration of a thorough understanding</li> </ul> </li> </ul>		
1 Point	Point       A one-point response demonstrates only a partial understanding of the mathematical concepts and/or procedures in the task.         This response       • correctly addresses only some elements of the task         • may contain an incorrect solution but applies a mathematically appropriate process         • may contain the correct solution but required work incomplete		
0 Point*	A zero-point response is incorrect, irrelevant, incoherent, or contains a correct solution obtained using an obviously incorrect procedure. Although some elements may contain correct mathematical procedures, holistically they are not sufficient to demonstrate even a limited understanding of the mathematical concepts embodied in the task.		

\*Condition Code A is applied whenever a student who is present for a test session leaves an entire constructed-response question in that session completely blank (no response attempted).

	3-Point Holistic Rubric
Score Points	
3 Point	<ul> <li>A three-point response includes the correct solution(s) to the question and demonstrates a thorough understanding of the mathematical concepts and/or procedures in the task.</li> <li>This response</li> <li>indicates that the student has completed the task correctly, using mathematically sound procedures</li> <li>contains sufficient work to demonstrate a thorough understanding of the mathematical concepts and/or procedures</li> </ul>
	<ul> <li>may contain inconsequential errors that do not detract from the correct solution(s) and the demonstration of a thorough understanding</li> </ul>
2 Point	A two-point response demonstrates a partial understanding of the mathematical concepts and/or procedures in the task.
	This response
	<ul> <li>appropriately addresses most, but not all aspects of the task using mathematically sound procedures</li> <li>may contain an incorrect solution but provides sound procedures, reasoning, and/or explanations</li> <li>may reflect some minor misunderstanding of the underlying mathematical concepts and/or procedures</li> </ul>
1 Point	A one-point response demonstrates only a limited understanding of the mathematical concepts and/or procedures in the task.
	<ul> <li>This response</li> <li>may address some elements of the task correctly but reaches an inadequate solution and/or provides reasoning that is faulty or incomplete</li> <li>exhibits multiple flaws related to misunderstanding of important aspects of the task, misuse of mathematical procedures, or faulty mathematical reasoning</li> <li>reflects a lack of essential understanding of the underlying mathematical concepts</li> <li>may contain the correct solution(s) but required work is limited</li> </ul>
0 Point*	A zero-point response is incorrect, irrelevant, incoherent, or contains a correct solution obtained using an obviously incorrect procedure. Although some elements may contain correct mathematical procedures, holistically they are not sufficient to demonstrate even a limited understanding of the mathematical concepts embodied in the task.

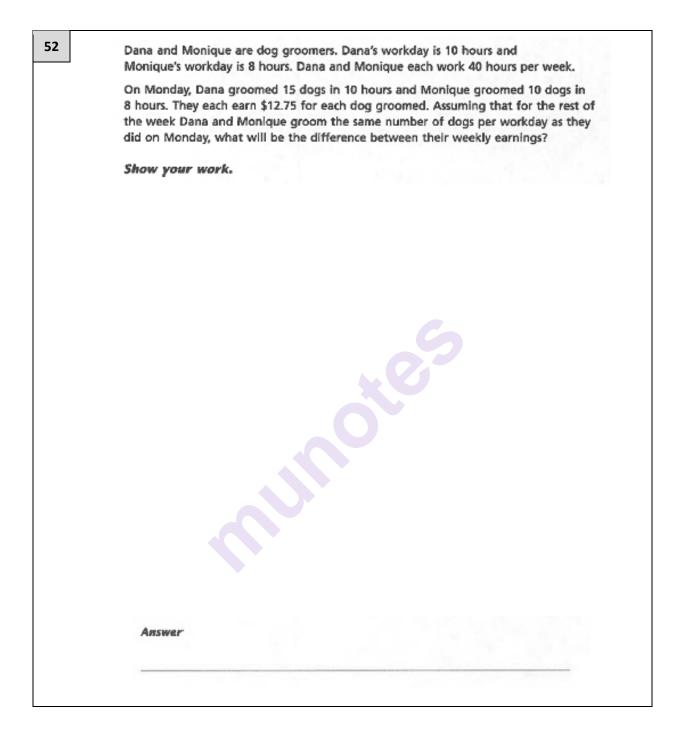
#### **3-Point Holistic Rubric**

\*Condition Code A is applied whenever a student who is present for a test session leaves an entire constructed-response question in that session completely blank (no response attempted).

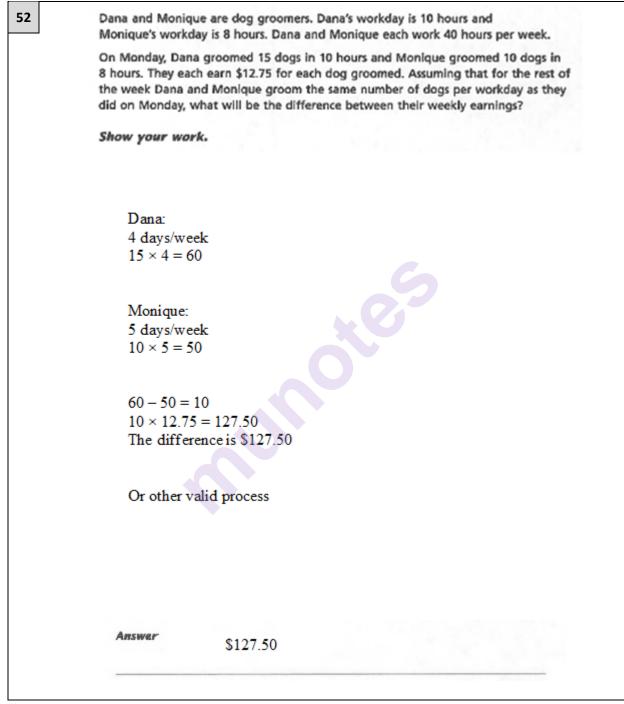
#### 2017 2- and 3-Point Mathematics Scoring Policies

Below are the policies to be followed while scoring the mathematics tests for all grades:

- 1. If a student shows the work in other than a designated "Show your work" or "Explain" area, that work should still be scored.
- If the question requires students to show their work, and the student shows appropriate work and clearly identifies a correct answer but fails to write that answer in the answer blank, the student should still receive full credit.
- If students are directed to show work, a correct answer with no work shown receives no credit.
- 4. If students are **not** directed to show work, any work shown will **not** be scored. This applies to items that do **not** ask for any work and items that ask for work for one part and do **not** ask for work in another part.
- If the student provides one legible response (and one response only), the rater should score the response, even if it has been crossed out.
- 6. If the student has written more than one response but has crossed some out, the rater should score only the response that has **not** been crossed out.
- Trial-and-error responses are not subject to Scoring Policy #6 above, since crossing out is part of the trial-and-error process.
- If a response shows repeated occurrences of the same conceptual error within a question, the conceptual error should **not** be considered more than once in gauging the demonstrated level of understanding.
- In questions requiring number sentences, the number sentences must be written horizontally.
- 10. Condition Code A is applied whenever a student who is present for a test session leaves an entire constructed-response question in that session completely blank (no response attempted). This is not to be confused with a score of zero wherein the student does respond to part or all of the question but that work results in a score of zero.



### **EXEMPLARY RESPONSE**





Dana and Monique are dog groomers. Dana's workday is 10 hours and Monique's workday is 8 hours. Dana and Monique each work 40 hours per week.
On Monday, Dana groomed 15 dogs in 10 hours and Monique groomed 10 dogs in 8 hours. They each earn \$12.75 for each dog groomed. Assuming that for the rest of the week Dana and Monique groom the same number of dogs per workday as they did on Monday, what will be the difference between their weekly earnings?
Show your work.
Dana: \$765 a week
40÷10=4 days a week
\$12.75 × 15 dogs = \$191.25 ~ one day
\$191.25 × 4 days = \$765 ← a week
Maria State Contract
Monique: \$637.50 a week
40÷ 8 = 5 days a week \$12.75 × 10 dogs = \$127.50 + one day \$127.50 × 5 days = \$637.50 = a week
\$12.75 × 10 dogs = \$127.50 + one oldg
\$127.50 × 5 days = \$631.502 4 4000
\$765 - \$637.50 - \$127.50
Answer
\$127.50

#### Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The weekly earnings of both groomers and the difference between their earnings are correctly determined using mathematically sound procedures.

Г

Monday, what will be the difference between their weekly earnings?
15-4 = 60 × 12.75=5765
10.5 = 50 × 12.75\$6375
765.0 - 6375
124.5
1045

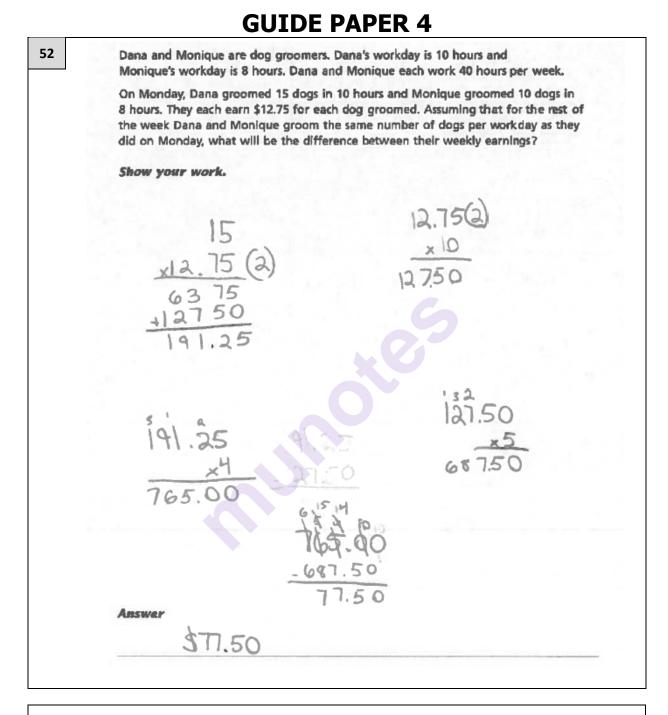
#### Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The weekly earnings of both groomers and the difference between their earnings are correctly determined using mathematically sound procedures.

2	
	Dana and Monique are dog groomers. Dana's workday is 10 hours and Monique's workday is 8 hours. Dana and Monique each work 40 hours per week.
	On Monday, Dana groomed 15 dogs in 10 hours and Monique groomed 10 dogs in 8 hours. They each earn \$12.75 for each dog groomed. Assuming that for the rest of the week Dana and Monique groom the same number of dogs per workday as they did on Monday, what will be the difference between their weekly earnings?
	Show your work.
	DI 15-4=60
	M 10.5=50 75
	60-50=10
	\$12.75.10 €127.50
	Answer \$ 127,50

#### Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The difference in the number of dogs groomed per week is correctly calculated, and the difference between earnings is correctly determined using mathematically sound procedures.



#### Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts in the task. Dana's weekly earnings are calculated correctly; however, a calculation error occurs when determining Monique's weekly earnings ( $127.5 \times 5$ ), resulting in an incorrect final solution. The response contains an incorrect solution but applies a mathematically appropriate process.

did on Monday	a and Monique groom the y, what will be the differe			
Show your w	13750	· 12.	15	
	x 15	+ 129	50	
	+12750	\$T27	50	
	\$191.25	6		
		101 25		
		-127.5	2	
		163.1	2	
Answer				

#### Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts in the task. The difference between daily earnings rather than weekly earnings is calculated. The response correctly addresses only some elements of the task.

Dana and Monique are dog groomers. Dana's workday is 10 h Monique's workday is 8 hours. Dana and Monique each work	
On Monday, Dana groomed 15 dogs in 10 hours and Monique 8 hours. They each earn \$12.75 for each dog groomed. Assumi the week Dana and Monique groom the same number of dogs did on Monday, what will be the difference between their week	ng that for the rest of per workday as they
Show your work.	
D-4daus	
D= 4 days M= B days	
M= 5 daup	
	101 20
	191.23
	127.5
	710
	765
	637.5
Answer	
The difference is	127 50.

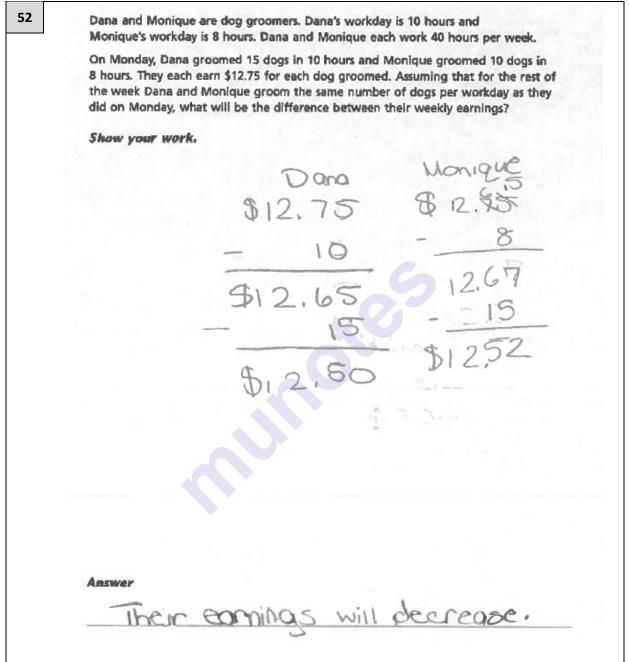
#### Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts in the task. Although correct answers are provided for daily and weekly earnings as well as the difference between weekly earnings, the response contains limited work to support them. The response contains the correct solution but required work is incomplete.

Dans and Maximus and day any many Barris and a start
Dana and Monique are dog groomers. Dana's workday is 10 hours and Monique's workday is 8 hours. Dana and Monique each work 40 hours per week.
On Monday, Dana groomed 15 dogs in 10 hours and Monique groomed 10 dogs in 8 hours. They each earn \$12.75 for each dog groomed. Assuming that for the rest of the week Dana and Monique groom the same number of dogs per workday as they did on Monday, what will be the difference between their weekly earnings?
Show your work.
132
63-75
191.25
Answer

#### Score Point 0 (out of 2 points)

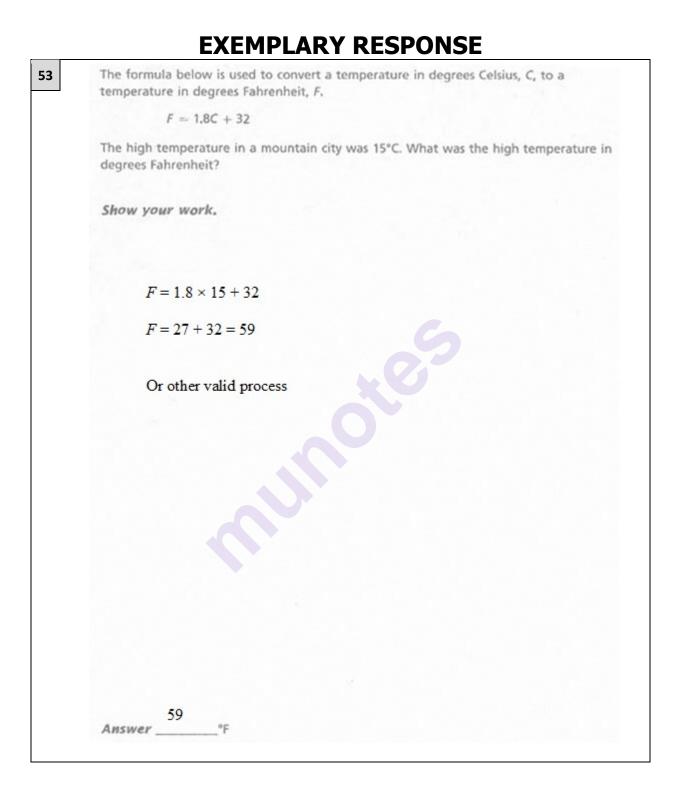
Although Dana's daily earnings are calculated correctly, holistically this calculation alone is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task.



#### Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. An incorrect procedure of subtracting hours from dollars is used to determine the solution.

53 The formula below is used to convert a temperature in degrees Celsius, C, to a temperature in degrees Fahrenheit, F. F = 1.8C + 32The high temperature in a mountain city was 15°C. What was the high temperature in degrees Fahrenheit? Show your work. Answer \_\_\_\_\_°F



53	The formula below is used to convert a temperature in degrees Celsius, C, to a temperature in degrees Fahrenheit, F.
	F = 1.8C + 32
	The high temperature in a mountain city was 15°C. What was the high temperature in degrees Fahrenheit?
	Show your work.
	F = 1.8(+32) (59°F)
	F = 1.8(15) + 32
	F = 27 + 32
	F= 59
	50
	Answer 59 of

#### Score Point 2 (out of 2 points)

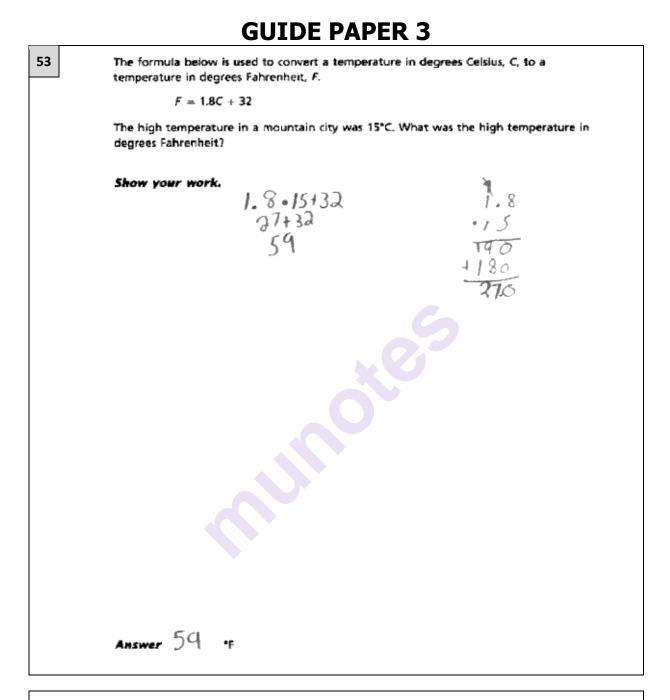
This response demonstrates a thorough understanding of the mathematical concepts in the task. The response correctly uses the given formula to convert the high temperature to degrees Fahrenheit.

<b>GUIDE PAPER</b>	2
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53	The formula below is used to convert a temperature in degrees Celsius, C, to a temperature in degrees Fahrenheit, F.
	F = 1.8C + 32
	The high temperature in a mountain city was 15°C. What was the high temperature in degrees Fahrenheit?
	Show your work.
	F=1.8.15+32
	(59°F)
	Answer 59 +F

#### Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The response correctly uses the given formula to convert the high temperature to degrees Fahrenheit.



#### Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The response correctly uses the given formula to convert the high temperature to degrees Fahrenheit.

53	The formula below is used to convert a temperature in degrees Celsius, C, to a temperature in degrees Fahrenheit, $F_{-}$
	F = 1.8C + 32
	The high temperature in a mountain city was 15°C. What was the high temperature in degrees Fahrenheit?
	Show your work.
	F=1.8C+300 ×1.8
	F=1.8×15+32 100
	F= 270+32
	F= 302
	Answer 3000 *F

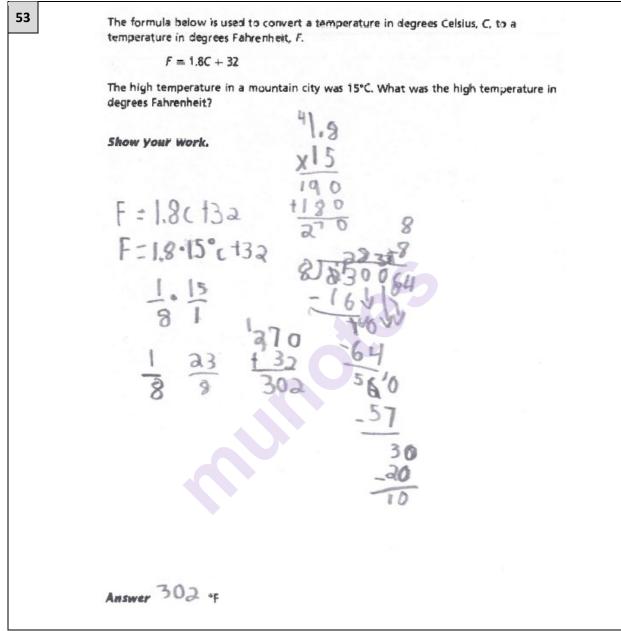
#### Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts in the task. This response contains a correct equation ( $F = 1.8 \times 15 + 32$ ); however, there is a calculation error in solving for the degrees Fahrenheit, ( $1.8 \times 15 = 270$ ). This response contains an incorrect solution but applies a mathematically appropriate process.

3	The formula below is used to convert a temperature in degrees Celsius, C, to a
	temperature in degrees Fahrenheit, F.
	F = 1.8C + 32
	The high temperature in a mountain city was 15°C. What was the high temperature in degrees Fahrenheit?
	Show your work.
	1.8×15 7.8 (27 °F)
	90
	180
	270
	27
	Answer 27 *F

#### Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts in the task. The response correctly multiples 1.8 and 15 to get 27°; however, the constant in the formula is omitted while converting from degrees of Celsius to degrees of Fahrenheit. This response correctly addresses only some elements of the task.



#### Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts in the task. This response contains a correct equation ( $F = 1.8 \cdot 15^{\circ}c + 32$ ); however, there is a calculation error in solving for the degrees Fahrenheit, ( $1.8 \times 15 = 270$ ). This response contains an incorrect solution but applies a mathematically appropriate process.

53	The formula below is used to convert a temperature in degrees Celsius, C, to a temperature in degrees Fahrenheit, F.
	F = 1.8C + 32
	The high temperature in a mountain city was 15°C. What was the high temperature in degrees Fahrenheit?
	Show your work.
	32+1.8(15)
	32+1.8(15) 33.8×15
	507
	Answer 507 of

#### Score Point 0 (out of 2 points)

Although this response correctly writes the expression to convert to degrees Fahrenheit, the student does not apply the order of operations properly. Holistically this response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task.

#### Additional

53	The formula below is used to convert a temperature in degrees Celsius, C, to a temperature in degrees Fahrenheit, F.
	F = 1.8C + 32
	The high temperature in a mountain city was 15°C. What was the high temperature in degrees Fahrenheit?
	Show your work.
	15=1.8=8.3
	8.3+32=40.3
	40.3°F
	Answer *F

#### Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. This response incorrectly divides 15 by 1.8.

54	A seamstress needs to cut 15-inch pieces of ribbon from a roll of ribbon that is 9 feet in length. What is the greatest number of 15-inch pieces the seamstress can cut from 5 of these rolls of ribbon?
	Show your work.
	Answer pieces

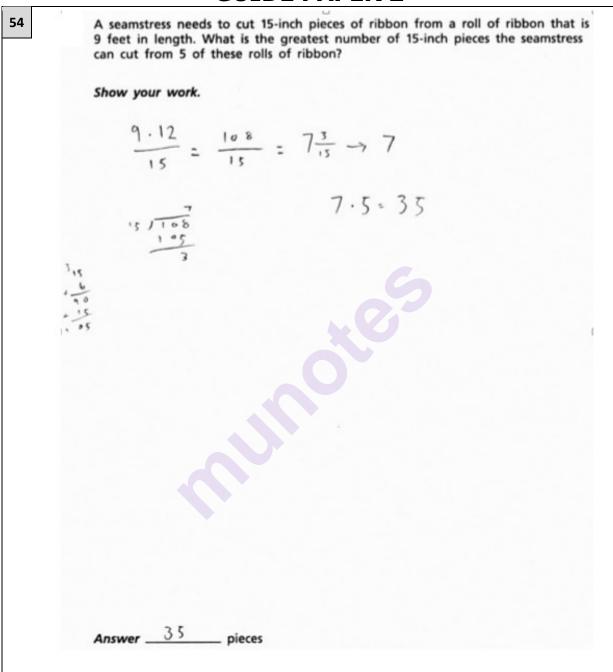
### **EXEMPLARY RESPONSE**

54	A seamstress needs to cut 15-inch pieces of ribbon from a roll of ribbon that is 9 feet in length. What is the greatest number of 15-inch pieces the seamstress can cut from 5 of these rolls of ribbon?
	Show your work.
	9 feet $\times$ 12 inches = 108 inches per roll of ribbon
	$108 \div 15 = 7.2$ pieces per roll
	$7 \times 5 = 35$ pieces
	Or other valid process
	Answer pieces

	GUIDE PAPER 1	Additional
54	A seamstress needs to cut <u>15-inch</u> pieces of ribbon from a roll 9 feet in length. What is the greatest number of 15-inch piece can cut from 5 of these rolls of ribbon?	
	Show your work.	
	$ \begin{array}{c} \textcircledleft{1} = 17 \text{ in.} \\ 9\text{ ff} = 108 \text{ in.} \\ 15/108 \text{ in.} \\ 15/108 \text{ in.} \\ 15/108 \text{ in.} \\ 105 \text{ in.} \\ 105 \end{array} $	
	,	
	73527	
	Answer 3 B pieces	

#### Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The number of pieces that can be cut from a single roll of ribbon is calculated correctly and appropriately multiplied to account for all 5 rolls of ribbon.



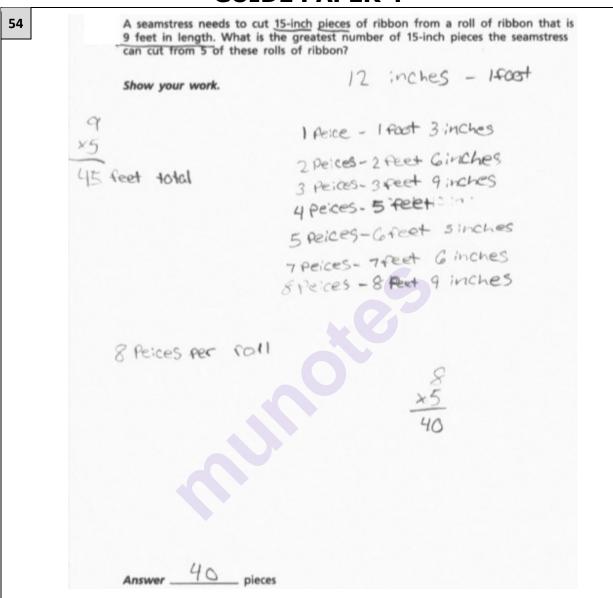
#### Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The number of pieces that can be cut from a single roll of ribbon is calculated correctly and appropriately multiplied to account for all 5 rolls of ribbon.

E A	
54	A seamstress needs to cut 15-inch pieces of ribbon from a roll of ribbon that is 9 feet in length. What is the greatest number of 15-inch pieces the seamstress can cut from 5 of these rolls of ribbon?
	Show your work.
	4541
	Avain -
	9 - 13 X12 - 35
	108 10712
	Answer 36 pieces
l	Answer 200 pieces

#### Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The number of pieces that can be cut from a single roll of ribbon is calculated correctly and appropriately multiplied to account for all 5 rolls of ribbon. As per Scoring Policy #6, the work that has been crossed out should not be considered in scoring.



#### Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts in the task. 15-inch pieces are cumulatively added until 9 feet is reached; however, the count of pieces skips from 5 pieces to 7 pieces, resulting in an incorrect number of pieces per roll. The result is then appropriately multiplied to account for all 5 rolls of ribbon. The response contains an incorrect solution but applies a mathematically appropriate process.

54	A seamstress needs to cut 15-inch pieces of ribbon from a roll of ribbon that is 9 feet in length. What is the greatest number of 15-inch pieces the seamstress can cut from 5 of these rolls of ribbon?
	Show your work.
	9.5.12
	45.12
	9.5.12 45.12 540 in. 540 - 15
	36)
	Answer pieces

#### Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts in the task. The total length in inches of all 5 rolls of ribbon is calculated correctly and appropriately divided by 15 to calculate the number of pieces that can be cut; however, this approach fails to account for each individual roll having some length of scrap material left over. The response correctly addresses only some elements of the task.

Show	your work.
	12 inches= 1 Foot
	17
	1 72
	XY ISIGS
	100
	108 772-7
	1. С.
· ·	7 Peros Initi
Answ	rer Z pieces 7 Pieces with Six in C-Besieft
	OVER INC-ARSIPT

#### Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts in the task. The number of pieces that can be cut from a single roll of ribbon is calculated correctly; however, this result is never multiplied to account for all 5 rolls of ribbon. The response correctly addresses only some elements of the task.

	GUIDE PAPER /
9 fe	amstress needs to cut 15-inch pieces of ribbon from a roll of ribbon that is et in length. What is the greatest number of 15-inch pieces the seamstress cut from 5 of these rolls of ribbon?
Show	v your work.
	9 45 *5 *15 45 675
Ann	ver <u>675</u> pieces

### 

#### Score Point 0 (out of 2 points)

Although some elements may contain correct mathematical procedures, holistically they are not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. The total length in feet of all 5 rolls of ribbon is calculated correctly; however, it is never converted into inches and is inappropriately multiplied by 15 rather than divided by 15.

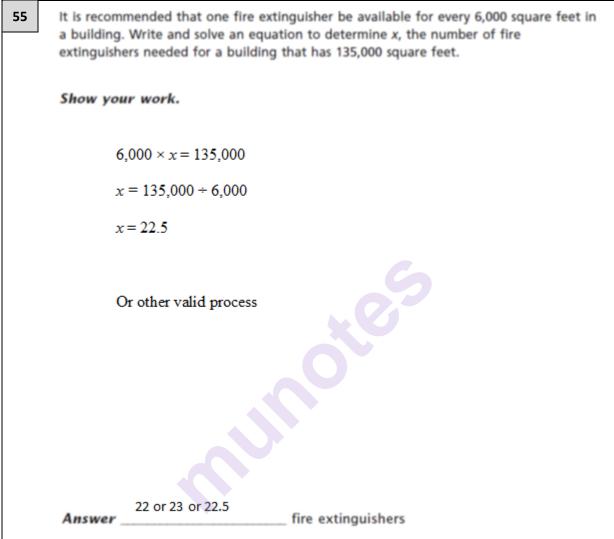
	GUIDE PAPER 8 Additio	nal
54	A seamstress needs to cut 15-inch pieces of ribbon from a roll of ribbon that is 9 feet in length. What is the greatest number of 15-inch pieces the seamstress can cut from 5 of these rolls of ribbon?	
	Show your work.	
	af-108 in	
	afri	
	5108	
	12	
	X 360	
	72	
	Answer pieces	

#### Score Point 0 (out of 2 points)

Although some elements may contain correct mathematical procedures, holistically they are not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. The length of one roll of ribbon is correctly converted to inches and then divided by 15 to calculate the number of pieces that can be cut; however, this result is never multiplied to account for all 5 rolls of ribbon and a decimal point is missing from the solution.

55	It is recommended that one fire extinguisher be available for every 6,000 square feet in a building. Write and solve an equation to determine <i>x</i> , the number of fire extinguishers needed for a building that has 135,000 square feet.
	Show your work.
	Answer fire extinguishers





	GUIDE PAPER 1	Additional
55	It is recommended that one fire extinguisher be available for every $6,0$ a building. Write and solve an equation to determine $x$ , the number o extinguishers needed for a building that has 135,000 square feet.	
	Show your work.	
	6,000 × = 135,000 4000	22.5
	Answer 23 fire extinguishers	

This response demonstrates a thorough understanding of the mathematical concepts in the task. The equation is correctly written and solved with the appropriate answer indicated. This response indicates that the student has completed the task correctly, using mathematically sound procedures.

5		
		inguisher be available for every 6,000 square feet in ation to determine <i>x</i> , the number of fire that has 135,000 square feet.
	Show your work.	
	6000 x2 = 12000 6000 x5 = 20,000	6000×x=135,000 b000×225=135000
	6000x7= 396,000 6000x66= 132,000	
	6000×123= 138,000 6000×22.5= 135,000 6000×22.5= 135,000	
	22.5	
	Answer 22.5	fire extinguishers

### Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The correct equation is provided along with the correct solution.

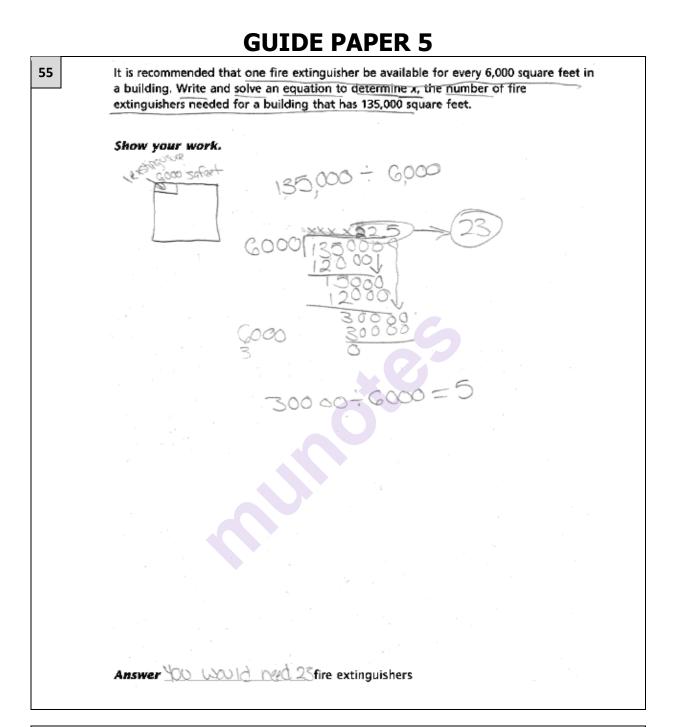
55	It is recommended that one fire extinguisher be available for every 6,00 a building. Write and solve an equation to determine x, the number of extinguishers needed for a building that has 135,000 square feet.	
	Show your work.	
	6,009)X=135,000	
	6309135,000 18 15	
	30	
	Answer 22 fire extinguishers	

#### Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The equation is correctly written and solved with the appropriate answer indicated. This response indicates that the student has completed the task correctly, using mathematically sound procedures.

a building. Write and solv	ne fire extinguisher be available for every 6,000 square fee re an equation to determine <i>x</i> , the number of fire a building that has 135,000 square feet.
Show your work.	
G,000	$x = 135,000 \div 6,000$
	6 (1.33.9, 135, 200
6,000	15 -12 30
12 00 00 C	
Answer 22.	-

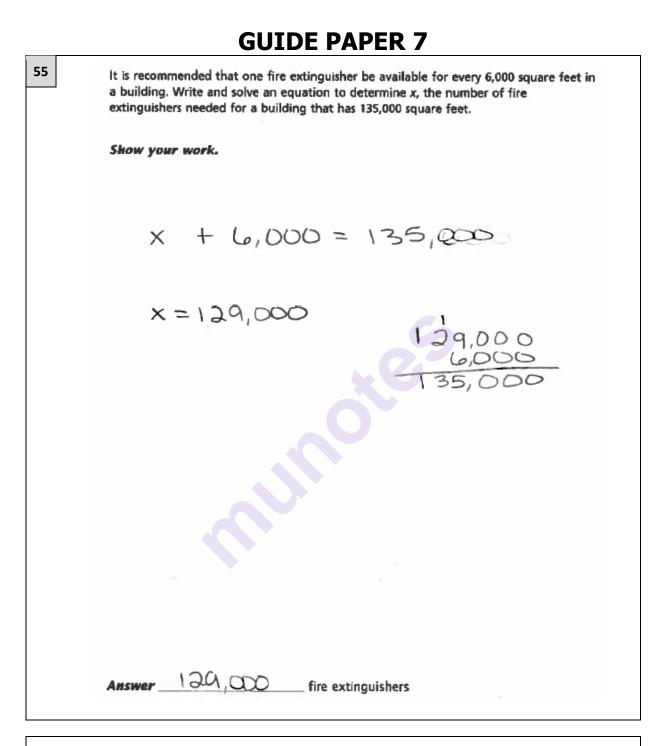
This response demonstrates only a partial understanding of the mathematical concepts in the task. The number of fire extinguishers is correctly determined; however, an incorrect equation is provided to solve for the solution. This response correctly addresses only some elements of the task.



This response demonstrates only a partial understanding of the mathematical concepts in the task. The response correctly solves for the proper number of fire extinguishers  $(135,000 \div 6,000)$ ; however, an equation is not provided. This response contains the correct solution but required work is incomplete.

GUIDE PAPER 6		
It is recommended that one fire extinguisher be available for every 6,000 square feet in a building. Write and solve an equation to determine <i>x</i> , the number of fire extinguishers needed for a building that has 135,000 square feet.		
Show your work. 22.5 60001135,000		
Answer 22.5 fire extinguishers		

This response demonstrates only a partial understanding of the mathematical concepts in the task. The response correctly solves for the proper number of fire extinguishers; however, an equation is not provided. This response correctly addresses only some elements of the task.

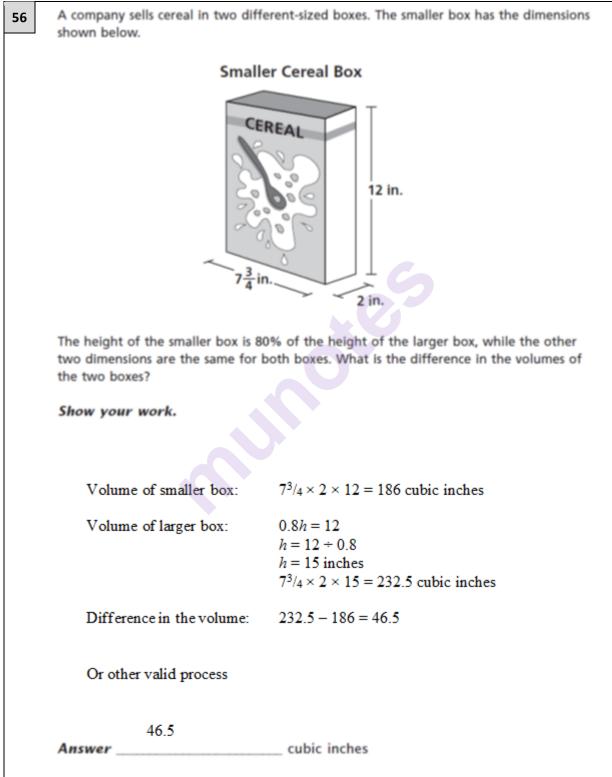


Holistically, this response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. The equation written is incorrect and is used to determine the incorrect number of fire extinguishers.

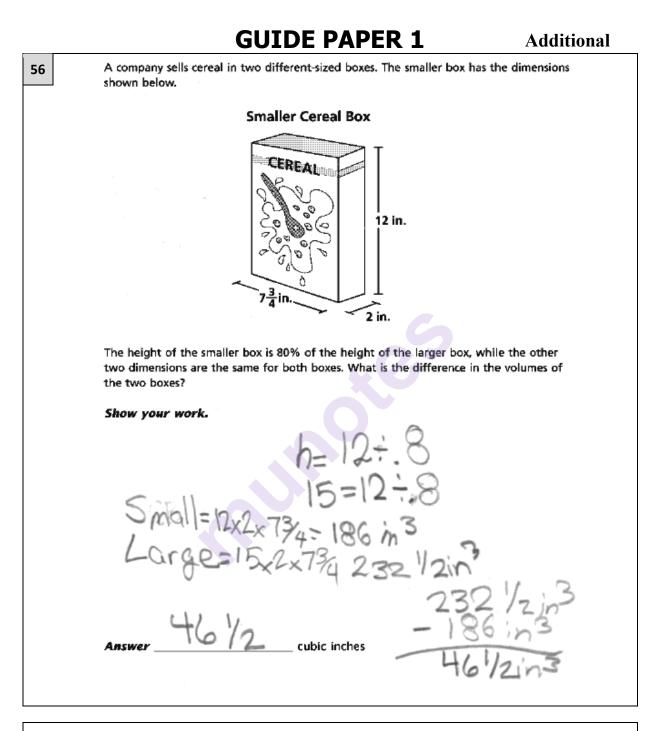
**GUIDE PAPER 8** Additional It is recommended that one fire extinguisher be available for every 6,000 square feet in 55 a building. Write and solve an equation to determine x, the number of fire extinguishers needed for a building that has 135,000 square feet. Show your work. Answer 14 000 fire extinguishers

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. Values from the prompt are inappropriately added.

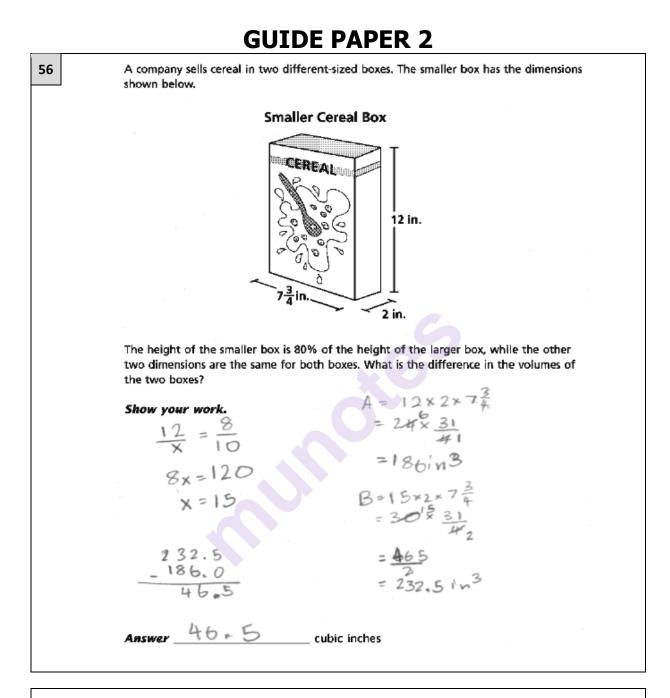
56	A company sells cereal in two different-sized boxes. The smaller box has the dimensions shown below.
	Smaller Cereal Box
	$7\frac{3}{4}$ in. $2$ in.
	The height of the smaller box is 80% of the height of the larger box, while the other two dimensions are the same for both boxes. What is the difference in the volumes of the two boxes?
	Show your work.
	Answer cubic inches



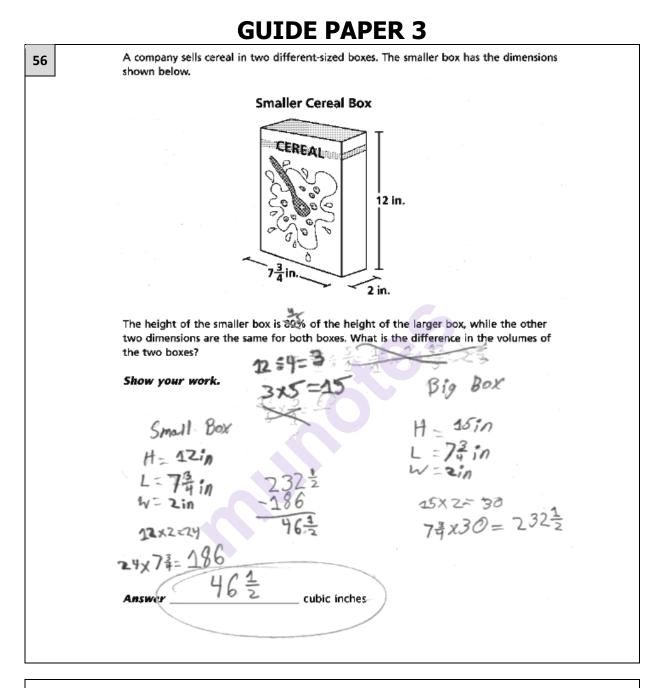
## **EXEMPLARY RESPONSE**



This response demonstrates a thorough understanding of the mathematical concepts in the task. The response correctly determines the volume of both cereal boxes and then subtracts for a correct solution of the difference in the volumes. This response indicates that the student has completed the task correctly, using mathematically sound procedures.



This response demonstrates a thorough understanding of the mathematical concepts in the task. The response uses ratios to correctly determine the height of the larger box. The volume of both cereal boxes is correctly calculated and the difference in the volumes is determined for the correct solution. This response indicates that the student has completed the task correctly, using mathematically sound procedures.

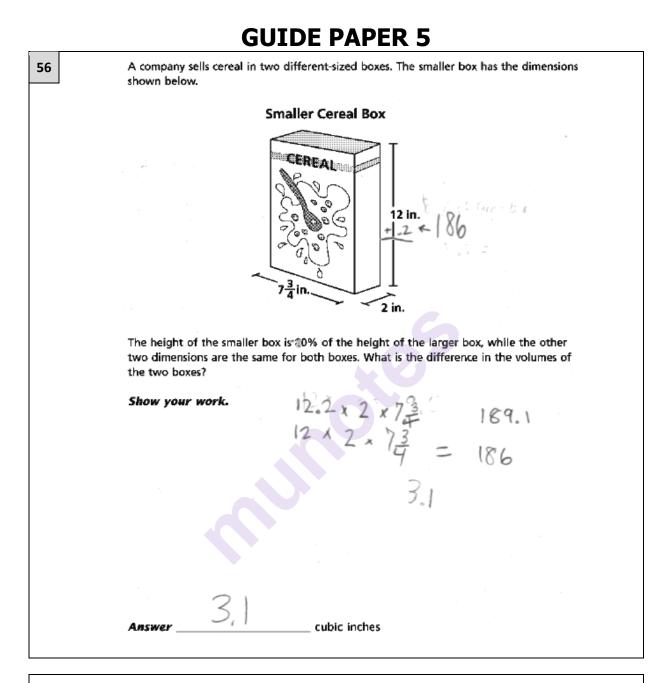


This response demonstrates a thorough understanding of the mathematical concepts in the task. The response correctly determines the volume of both cereal boxes and then subtracts for a correct solution of the difference in the volumes. As per Scoring Policy #6, if the student has written more than one response but has crossed some out, raters should score only the response that has not been crossed out.

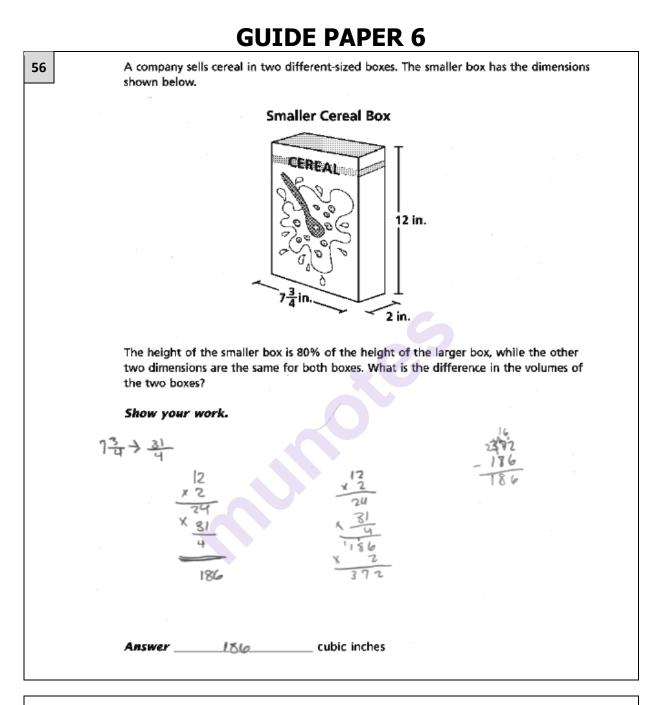
56 A company sells cereal in two different-sized boxes. The smaller box has the dimensions shown below. Smaller Cereal Box REAL 12 in. 2 in. The height of the smaller box is 80% of the height of the larger box, while the other two dimensions are the same for both boxes. What is the difference in the volumes of the two boxes? 5.5 Show your work. = 12x2x 7.75= 7.75 = 235.5 cubic inches Answei

### Score Point 1 (out of 2 points)

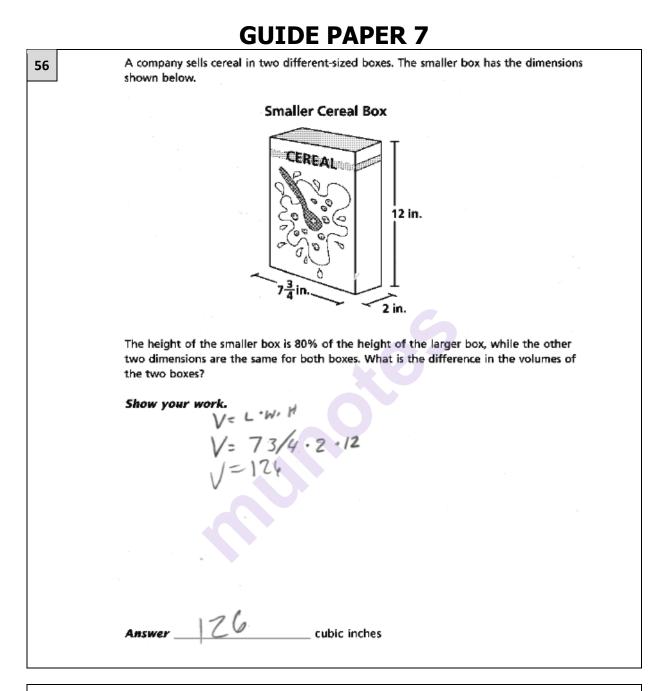
This response demonstrates only a partial understanding of the mathematical concepts in the task. The volume of the smaller cereal box is correctly calculated; however, the work for the volume of the larger cereal box contains a calculation error. This response contains an incorrect solution but applies a mathematically appropriate process.



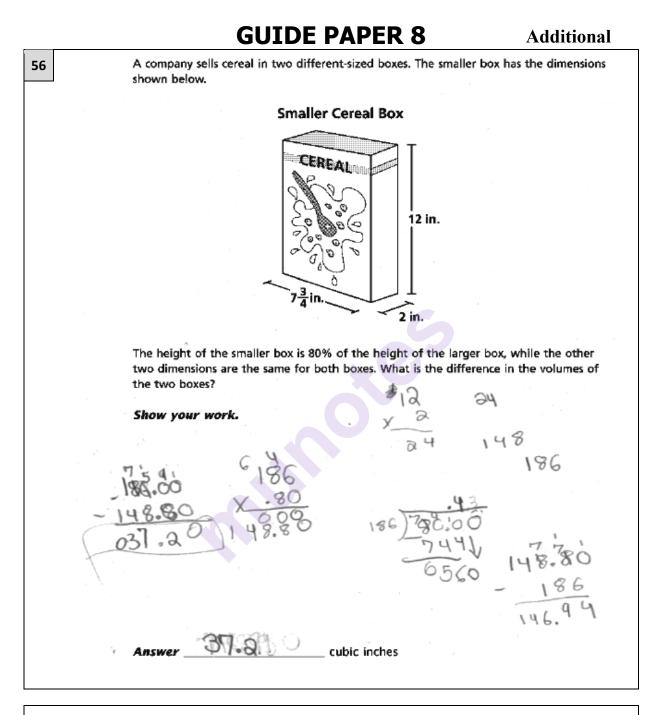
This response demonstrates only a partial understanding of the mathematical concepts in the task. The volume of the smaller cereal box is correctly calculated; however, the height of the larger cereal box is incorrect resulting in an incorrect volume of the larger cereal box. The difference between the two volumes is then used to determine the solution. This response contains an incorrect solution but applies a mathematically appropriate process.



This response demonstrates only a partial understanding of the mathematical concepts in the task. The volume of the smaller cereal box is correctly calculated. The volume of the larger cereal box is calculated incorrectly  $(186 \times 2)$ , then the difference between the two volumes is determined for the solution. This response contains an incorrect solution but applies some mathematically appropriate processes.



Holistically this response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. Although the equation for the volume of the small cereal box is correctly shown, it contains a calculation error and no other work is provided.



Holistically this response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. The volume of the smaller box is shown; however, it is unclear how it was calculated. The other work contains multiple incorrect procedures that demonstrate no understanding of how to use this value.

57	The area of Brian's rectangular garden, in square feet, can be found by using the expression $6(2x+5y)$ . Use the distributive property to write an equivalent expression for the area of Brian's garden.
	Equivalent expression
	Use your equivalent expression to find the area of Brian's garden, in square feet, if $x = 3$ and $y = 4$ .
	Show your work.
	Area square feet

### **EXEMPLARY RESPONSE**

57 The area of Brian's rectangular garden, in square feet, can be found by using the expression 6(2x+5y). Use the distributive property to write an equivalent expression for the area of Brian's garden. 12x + 30yEquivalent expression \_\_\_\_ Use your equivalent expression to find the area of Brian's garden, in square feet, if x = 3 and y = 4. Show your work. 12(3) + 30(4)36 + 120156 Or other valid process 156 square feet Area

expression $6(2x+5y)$ . for the area of Brian's		quivalent expressio
Equivalent expression	(12x)+BOY)	
Use your equivalent exists if $x = 3$ and $y = 4$ .	xpression to find the area of Brian's garden	, in square feet,
Show your work.	12(3) + 30(4)	
	36+120	
	156	
15		

This response demonstrates a thorough understanding of the mathematical concepts in the task. The distributive property is correctly applied to the expression to construct an equivalent expression. This equivalent expression is used to correctly solve for the area of the garden. This response indicates that the student has completed the task correctly, using mathematically sound procedures.

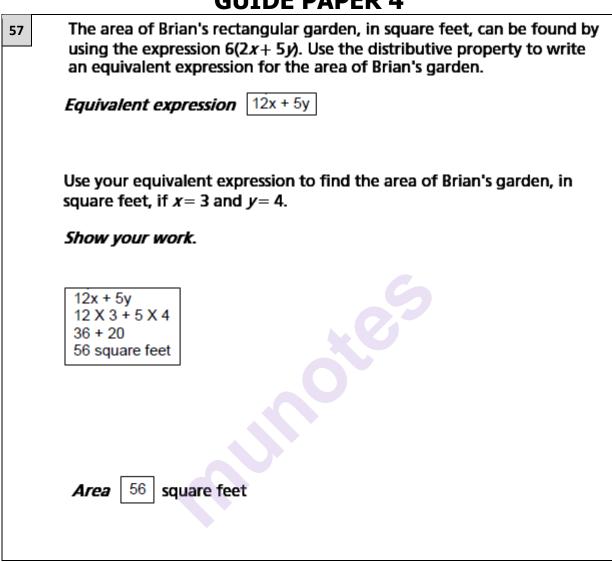
57	The area of Brian's rectangular garden, in square feet, can be found by using the expression $6(2x + 5y)$ . Use the distributive property to write an equivalent expression for the area of Brian's garden.
	Equivalent expression 12x+30y
	Use your equivalent expression to find the area of Brian's garden, in square feet, if $x = 3$ and $y = 4$ .
	Show your work.
	12(3)+30(4) 36+120=156
	Area 156 square feet

### Score Point 2 (out of 2 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The distributive property is correctly applied to the expression to construct an equivalent expression. This equivalent expression is used to correctly solve for the area of the garden.

exp for	ression 6(2x+5y). Use the distributive property to write an equivalent express the area of Brian's garden. 6(2x+5y)
Equ	ivalent expression $6(1x+0y)$ 12x+30y
Use if x	your equivalent expression to find the area of Brian's garden, in square feet, = 3 and $y = 4$ .
Sho	w your work.
	12×3=36
	30x4=120
	120+36=156
<u>م</u> ر	a <u>156</u> square feet

This response demonstrates a thorough understanding of the mathematical concepts in the task. The distributive property is correctly applied to the expression to construct an equivalent expression. This equivalent expression is used to correctly solve for the area of the garden.



### Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts in the task. The value of 6 is only distributed to the term 2x rather than to both terms within the parentheses; as a result, the expression is not equivalent to the given expression. The student then correctly solves for the area of the garden using the expression they created. As per Scoring Policy #8, if a response shows repeated occurrences of the same conceptual error within a question, the conceptual error should not be considered more than once in gauging the demonstrated level of understanding.

Γ

using the expression 6(2)	ngular garden, in square feet, can be found by $x + 5y$ ). Use the distributive property to write a r the area of Brian's garden.
Equivalent expression	{12X+30Y}
	ression to find the area of Brian's garden, in
square feet, if $x = 3$ and	<i>y</i> = 4.
Show your work.	
(NO STUDENT RESPON	SE GIVEN)
Area 156 square feet	

### Score Point 1 (out of 2 points)

This response demonstrates only a partial understanding of the mathematical concepts in the task. The distributive property is correctly applied to construct an equivalent expression; however, no work is provided for the calculation of the area for the garden. This response correctly addresses only some elements of the task.

GUIDE PAPER 6
The area of Brian's rectangular garden, in square feet, can be found by using the expression $6(2x+5y)$ . Use the distributive property to write an equivalent expression for the area of Brian's garden. Equivalent expression $6(4x+2y+6)$
Use your equivalent expression to find the area of Brian's garden, in square feet, if $x = 3$ and $y = 4$ .
Show your work.
6(2x+5y)=156
6×26=156
$G\left(4x + 2y + 6\right)$
156
Area square feet

This response demonstrates only a partial understanding of the mathematical concepts in the task. This response follows a correct procedure to determine the solution of 156 square feet; however, the expression provided is not equivalent. This response correctly addresses only some elements of the task.

57	The area of Brian's rectangular garden, in square feet, can be found by using the expression $6(2x + 5y)$ . Use the distributive property to write an equivalent expression for the area of Brian's garden.
	Equivalent expression 1[6(2X+5Y)]
	Use your equivalent expression to find the area of Brian's garden, in square feet, if $x = 3$ and $y = 4$ .
	Show your work.
	(NO STUDENT RESPONSE GIVEN)

Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. The expression provided is copied from the prompt, multiplied by 1 and does not use the distributive property. Although the final solution is correct, as per Scoring Policy # 3, if students are directed to show work, a correct answer with no work shown receives no credit.

#### Additional

	nt expression $(6(5y + 7x))$
Use your if $x = 3$ a	equivalent expression to find the area of Brian's garden, in square feet, and $y = 4$ .
Show yo	ur work.
	5yx420+626 2xX36
	6(26

### Score Point 0 (out of 2 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. The expression is copied from the prompt and work is incorrect.

58	A hotel has a number of meeting rooms, $m$ , available for events. Each meeting room has 325 chairs. Write an equation to represent $c$ , the total number of chairs, in all of the meeting rooms at the hotel.
	Equation
	If $m = 7$ use your equation to find the total number of chairs in all of the meeting rooms at the hotel.
	Show your work.
	Answer chairs

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# **EXEMPLARY RESPONSE**

58	A hotel has a number of meeting rooms, <i>m</i> , available for events. Each meeting room has 325 chairs. Write an equation to represent <i>c</i> , the total number of chairs, in all of the meeting rooms at the hotel.
	Equation $325m = c$
	If $m = 7$ use your equation to find the total number of chairs in all of the meeting rooms at the hotel.
	Show your work.
	$325 \times 7 = c$
	2275 = c
	Or other valid process
	Answer 2275 chairs

		GU	IDE PAP	ER 1	Additional
58	meeting ro		airs. Write an	equation to	le for events. Each represent <i>c</i> , the total e hotel.
	Equation	C=325m			
		e your equatio g rooms at the		total number	r of chairs in all of
	Show you	r work.			
	7x325=22	275			
	Answer	2275	chairs		

This response demonstrates a thorough understanding of the mathematical concepts in the task. An appropriate equation is written and used to correctly solve for the total number of chairs. This response indicates that the student has used mathematically sound procedures.

	GUIDE PAPER 2
58	A hotel has a number of meeting rooms, <i>m</i> , available for events. Each meeting room has 325 chairs. Write an equation to represent <i>c</i> , the total number of chairs, in all of the meeting rooms at the hotel.
	Equation M.325=c
	If $m = 7$ use your equation to find the total number of chairs in all of the meeting rooms at the hotel.
	Show your work.
	325.7
	Answer 2275 chairs

This response demonstrates a thorough understanding of the mathematical concepts in the task. An appropriate equation is written and used to correctly solve for the total number of chairs. Although a period is used in place of a multiplication sign, this constitutes an inconsequential error that does not detract from the correct solution and the demonstration of a thorough understanding.

	GUIDE PAPER 3
meeting re	is a number of meeting rooms, <i>m</i> , available for events. Each oom has 325 chairs. Write an equation to represent <i>c</i> , the total f chairs, in all of the meeting rooms at the hotel.
Equation	m*325=c
	se your equation to find the total number of chairs in all of the ooms at the hotel.
Show you	r work.
3 2 5*7=	(7*5=35)+(7*20=140)+(7*300=2100)=2275
Answer	2275 chairs

This response demonstrates a thorough understanding of the mathematical concepts in the task. An appropriate equation is written and used to correctly solve for the total number of chairs. This response indicates that the student has used mathematically sound procedures.

	GUIDE PAPER 4
58	A hotel has a number of meeting rooms, <i>m</i> , available for events. Each meeting room has 325 chairs. Write an equation to represent <i>c</i> , the total number of chairs, in all of the meeting rooms at the hotel.
	Equation m325
	If $m = 7$ use your equation to find the total number of chairs in all of the meeting rooms at the hotel.
	Show your work.
	I multiplied 325 charis by the number of rooms which was 7 and got 2275 chairs total.
	Answer 2275 chairs

## DAD

### Score Point 2 (out of 3 points)

This response demonstrates a partial understanding of the mathematical concepts in the task. A correct solution is determined by appropriately multiplying the number of chairs by the number of meeting rooms; however, the work does not contain an equation, only an expression is provided. The response addresses most, but not all aspects of the task.

	GUIDE PAPER 5
58	A hotel has a number of meeting rooms, <i>m</i> , available for events. Each meeting room has 325 chairs. Write an equation to represent <i>c</i> , the total number of chairs, in all of the meeting rooms at the hotel.
	Equation 325x7=c
	If $m = 7$ use your equation to find the total number of chairs in all of the meeting rooms at the hotel.
	Show your work.
	325x7=2875 c=2875
	Answer 2875 chairs

This response demonstrates a partial understanding of the mathematical concepts in the task. An appropriate equation is written; however, the value of 7 is used in place of the variable m. The response contains an incorrect solution due to a calculation error, but provides sound procedures.

	GUIDE PAPER 6
58	A hotel has a number of meeting rooms, <i>m</i> , available for events. Each meeting room has 325 chairs. Write an equation to represent <i>c</i> , the total number of chairs, in all of the meeting rooms at the hotel.
	Equation 325timesM
	If $m = 7$ use your equation to find the total number of chairs in all of the meeting rooms at the hotel.
	Show your work.
	You have to multiply the # of meeting rooms by how many chairs are in each meeting room and it will equal 2275
	Answer 2275 chairs

## ITDE DADE

## Score Point 2 (out of 3 points)

This response demonstrates a partial understanding of the mathematical concepts in the task. A correct solution is determined by appropriately multiplying the number of chairs by the number of meeting rooms; however, only an expression is provided. The response addresses most, but not all aspects of the task.

	GOIDE PAPER /
58	A hotel has a number of meeting rooms, <i>m</i> , available for events. Each meeting room has 325 chairs. Write an equation to represent <i>c</i> , the total number of chairs, in all of the meeting rooms at the hotel.
	<b>Equation</b>
	If $m = 7$ use your equation to find the total number of chairs in all of the meeting rooms at the hotel.
	Show your work.
	7*325=1175
	Answer 1175 chairs

## Score Point 1 (out of 3 points)

This response demonstrates only a limited understanding of the mathematical concepts in the task. The number of chairs per meeting room is appropriately multiplied by the number of meeting rooms; however, the solution contains a calculation error and the equation provided is incorrect. This response exhibits multiple flaws related to misunderstanding of important aspects of the task.

		GUIDE PAPER 8	Additional
58	meeting room ha	mber of meeting rooms, <i>m</i> , availab as 325 chairs. Write an equation to , in all of the meeting rooms at th	represent <i>c</i> , the total
	Equation 7	x325=	
	If <i>m</i> = 7 use your the meeting room	equation to find the total numbers at the hotel.	er of chairs in all of
	Show your work	c.	
	7x 325=3275		
	Answer 32	75 chairs	

This response demonstrates only a limited understanding of the mathematical concepts in the task. A solution is determined by appropriately multiplying the number of chairs by the number of meeting rooms; however, the solution contains a calculation error and the equation provided is incomplete. This response addresses some elements of the task correctly but reaches an inadequate solution.

	GUIDE PAPER 9	
58	A hotel has a number of meeting rooms, <i>m</i> , available for events. Each meeting room has 325 chairs. Write an equation to represent <i>c</i> , the total number of chairs, in all of the meeting rooms at the hotel.	
	Equation C+(m*325)	
	If $m = 7$ use your equation to find the total number of chairs in all of the meeting rooms at the hotel.	
	Show your work.	
	(NO STUDENT RESPONSE GIVEN)	
	Answer 2275 chairs	

## ITDE DADE

## Score Point 1 (out of 3 points)

This response demonstrates only a limited understanding of the mathematical concepts in the task. A correct solution is determined by appropriately multiplying the number of chairs by the number of meeting rooms, which is related to the  $(m^*325)$ term shown; however, the expression provided is incorrect and is not an equation.

	GUIDE PAPER 10		
58	A hotel has a number of meeting rooms, <i>m</i> , available for events. Each meeting room has 325 chairs. Write an equation to represent <i>c</i> , the total number of chairs, in all of the meeting rooms at the hotel.		
	Equation m x c		
	If $m = 7$ use your equation to find the total number of chairs in all of the meeting rooms at the hotel.		
	Show your work.		
	(NO STUDENT RESPONSE GIVEN)		
	Answer 2275 chairs		

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. The expression provided does not support the final solution. Although the solution is correct, as per Scoring Policy #3, if students are directed to show work, a correct answer with no work shown receives no credit.

		<b>GUIDE PAPER 11</b>	Additional
58	meeting roo	a number of meeting rooms, <i>m</i> , ava m has 325 chairs. Write an equation hairs, in all of the meeting rooms at	to represent <i>c</i> , the total
	Equation	325/c=m	
		your equation to find the total num ms at the hotel.	ber of chairs in all of the
	Show your	vork.	
	325/c=m 325/c=7	325/7= 46.42857142857143 rour	nded 47
	Answer	47 chairs	

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. This response contains an incorrect solution obtained using an obviously incorrect procedure.

_		
!	1	Jimmy and his family are on their way to visit some family friends who live 780 miles away from them. Based on the route they chose, they expect to complete their trip in three days. The distances and average speeds for the first two days driven are shown below.
		<ul> <li>First day: 4 hours at an average speed of 60 miles per hour</li> </ul>
		<ul> <li>Second day: 6 hours at an average speed of 65 miles per hour</li> </ul>
		If the average speed on the third day is 60 miles per hour, how many more hours will it take for them to reach their family friends' home?
	1	Show your work.
	,	Answer hours

## **EXEMPLARY RESPONSE**

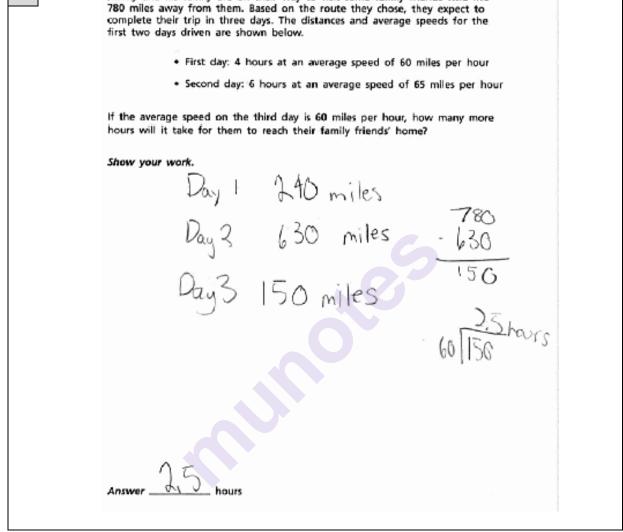
Γ

59	Jimmy and his family are on their way to visit some family friends who live 780 miles away from them. Based on the route they chose, they expect to complete their trip in three days. The distances and average speeds for the first two days driven are shown below.
	First day: 4 hours at an average speed of 60 miles per hour
	Second day: 6 hours at an average speed of 65 miles per hour
	If the average speed on the third day is 60 miles per hour, how many more hours will it take for them to reach their family friends' home?
	Show your work.
	4(60) + 6(65) + x(60) = 780
	240 + 390 + 60x = 780
	630 + 60x = 780
	60x = 150
	x = 2.5 hours
	Or other valid process
	Answer hours

# Jimmy and his family are on their way to visit some family friends who live

59

#### Additional



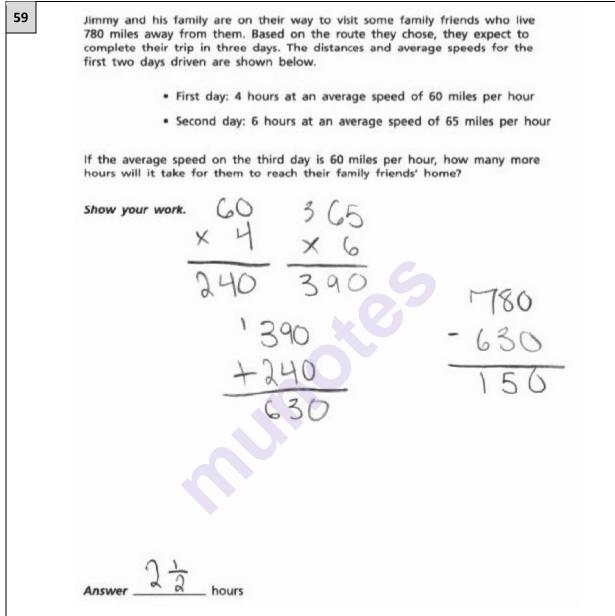
## Score Point 3 (out of 3 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The number of miles traveled on the first two days is correctly calculated and then subtracted from the total miles to determine the number of miles to be traveled on the third day. The speed from the third day is then used to correctly calculate the solution.

59	Jimmy and his family are on their way to visit some family friends who live 780 miles away from them. Based on the route they chose, they expect to complete their trip in three days. The distances and average speeds for the first two days driven are shown below.
	<ul> <li>First day: 4 hours at an average speed of 60 miles per hour</li> </ul>
	<ul> <li>Second day: 6 hours at an average speed of 65 miles per hour</li> </ul>
	If the average speed on the third day is 60 miles per hour, how many more hours will it take for them to reach their family friends' home?
	Show your work.
	4×60 = 240 miles
	& x & S = +390 miles
	530
	60/150 - 630 150
	2 · · ·
	Answer hours

#### Score Point 3 (out of 3 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The number of miles to be traveled on the third day is correctly calculated and the speed from the third day is then used to correctly calculate the solution. This response indicates that the student has used mathematically sound procedures.



#### Score Point 3 (out of 3 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The number of miles to be traveled on the third day is correctly calculated and a correct solution is determined, using mathematically sound procedures. The final division is performed mentally, which is acceptable.

## **GUIDE PAPER 4** 59 Jimmy and his family are on their way to visit some family friends who live 780 miles away from them. Based on the route they chose, they expect to complete their trip in three days. The distances and average speeds for the first two days driven are shown below. · First day: 4 hours at an average speed of 60 miles per hour · Second day: 6 hours at an average speed of 65 miles per hour If the average speed on the third day is 60 miles per hour, how many more hours will it take for them to reach their family friends' home? Show your work. Answer hours

## Score Point 2 (out of 3 points)

This response demonstrates a partial understanding of the mathematical concepts in the task. The number of miles to be traveled on the third day is correctly calculated; however, the solution of 2h 3m recorded on the answer blank is incorrect and not supported by the work shown. The response contains an incorrect solution but provides sound reasoning.

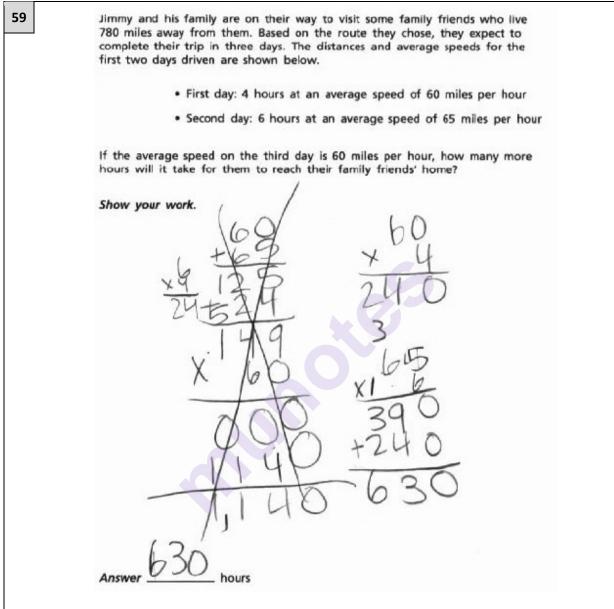
59	Jimmy and his family are on their way to visit some family friends who live 780 miles away from them. Based on the route they chose, they expect to complete their trip in three days. The distances and average speeds for the first two days driven are shown below.
	<ul> <li>First day: 4 hours at an average speed of 60 miles per hour</li> </ul>
	<ul> <li>Second day: 6 hours at an average speed of 65 miles per hour</li> </ul>
	If the average speed on the third day is 60 miles per hour, how many more hours will it take for them to reach their family friends' home? $G5$
	Show your work. $630$ $\frac{60}{\times 4}$ $\frac{\times 6}{390}$
	+ 60 lhr + 40 + 60 2hr + 240 + 60 2hr + 63 0
	Answer hours

#### Score Point 2 (out of 3 points)

This response demonstrates a partial understanding of the mathematical concepts in the task. The number of miles traveled on the first two days is correctly calculated. The speed for the third day is added to the total miles for the first two days until 750 miles is reached; however, 30 miles is unaccounted for and the 2 hours is misinterpreted as the final solution. The response appropriately addresses most, but not all aspects of the task using mathematically sound procedures.

	GUIDE PAPER 6
59	Jimmy and his family are on their way to visit some family friends who live 780 miles away from them. Based on the route they chose, they expect to complete their trip in three days. The distances and average speeds for the first two days driven are shown below.
	• First day: 4 hours at an average speed of 60 miles per hour
	Second day: 6 hours at an average speed of 65 miles per hour
	If the average speed on the third day is 60 miles per hour, how many more hours will it take for them to reach their family friends' home?
	show your work. 69 65 248
	100 - 310 - 100 - 5260 6300 - 100 - 6300
	Answer hours

This response demonstrates a partial understanding of the mathematical concepts in the task. The number of miles to be traveled on the third day is correctly calculated; however, the solution of 3 hours recorded on the answer blank is incorrect and it is unclear how it was obtained. The response contains an incorrect solution but provides sound reasoning.



#### Score Point 1 (out of 3 points)

This response demonstrates only a limited understanding of the mathematical concepts in the task. Although the total miles traveled on the first and second day are correctly calculated and added together; it was incorrectly interpreted as the final solution. This response exhibits multiple flaws related to misunderstanding of important aspects of the task. As per Scoring Policy #6, if the student has written more than one response but has crossed some out, raters should score only the response that has not been crossed out.

	GUIDE PAPER 8	Additional
59	Jimmy and his family are on their way to visit some family friends v 780 miles away from them. Based on the route they chose, they exp complete their trip in three days. The distances and average speeds first two days driven are shown below.	pect to
	<ul> <li>First day: 4 hours at an average speed of 60 miles p</li> </ul>	per hour
	<ul> <li>Second day: 6 hours at an average speed of 65 mile</li> </ul>	s per hour
	If the average speed on the third day is 60 miles per hour, how ma hours will it take for them to reach their family friends' home?	any more
	show your work.	× A D
	5	
	7 1	
	Answer hours	

This response demonstrates only a limited understanding of the mathematical concepts in the task. The total miles traveled on the first two days is correctly calculated and added together; however, no other work is shown. This response contains the correct solution but required work is limited.

59	Jimmy and his family are on their way to visit some family friends who live 780 miles away from them. Based on the route they chose, they expect to complete their trip in three days. The distances and average speeds for the first two days driven are shown below.
	• First day: 4 hours at an average speed of 60 miles per hour
	<ul> <li>Second day: 6 hours at an average speed of 65 miles per hour</li> </ul>
	If the average speed on the third day is 60 miles per hour, how many more hours will it take for them to reach their family friends' home?
	Show your work.
	6 65 30
	$\frac{\chi}{240} = \frac{\chi_6}{390}$
	-240 150
	. 37
	Answer 2.5 hours

## Score Point 1 (out of 3 points)

This response demonstrates only a limited understanding of the mathematical concepts in the task. The number of miles traveled on the first and second day is correctly calculated; however, the difference between the first day and second day is determined. This response addresses some elements of the task correctly but provides reasoning that is faulty.

59	Jimmy and his family are on their way to visit some family friends who live 780 miles away from them. Based on the route they chose, they expect to complete their trip in three days. The distances and average speeds for the first two days driven are shown below. • First day: 4 hours at an average speed of 60 miles per hour • Second day: 6 hours at an average speed of 65 miles per hour
	If the average speed on the third day is 60 miles per hour, how many more hours will it take for them to reach their family friends' home? <b>Show your work</b> .
	6 1780 -240 -240 540
	Answer <u>540</u> hours

#### Score Point 0 (out of 3 points)

The total miles traveled on the first day is correctly stated; however, the operation provided to show this calculation contains a transcription error for the speed traveled on the first day ( $6 \times 4 = 240$ ), which is technically not calculated correctly. This value is subtracted from the total distance, ignoring the total miles traveled on the second day, and the result is provided as the final solution. Holistically the response is not sufficient to demonstrate even a limited understanding of the mathematical concepts embodied in the task.

59 Jimmy and his family are on their way to visit some family friends who live 780 miles away from them. Based on the route they chose, they expect to complete their trip in three days. The distances and average speeds for the first two days driven are shown below. · First day: 4 hours at an average speed of 60 miles per hour · Second day: 6 hours at an average speed of 65 miles per hour If the average speed on the third day is 60 miles per hour, how many more hours will it take for them to reach their family friends' home? Show your work. 2 2 \$ 4 6 12 14 80 65 70 60 75 KS 9 Answer hours

#### Score Point 0 (out of 3 points)

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. The table provided incorrectly infers a pattern of 2 more hours at a speed of 5 more miles per hour each additional day.

A right rect	tangular prism has a length of $2\frac{1}{2}$ feet, a width of 3 feet, and a heig
	. Unit cubes with side lengths of $\frac{1}{2}$ foot are added to completely fill
the prism w	vith no space remaining. What is the volume, in cubic feet, of the righ
rectangular	prism?
Show your	work.
Answer	cubic feet
How many	$\frac{1}{2}$ -foot unit cubes can be added to fill the prism completely? Use what
you know a	about unit cubes or the side lengths of prisms to show your work or
explain you	r answer.

## **EXEMPLARY RESPONSE**

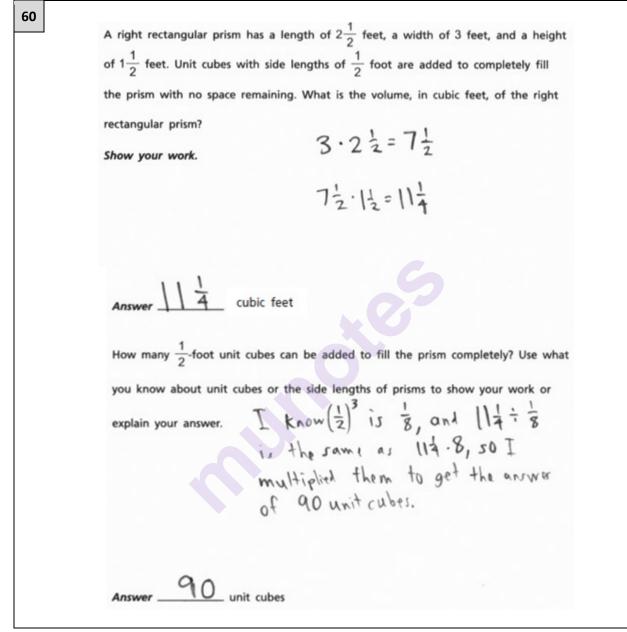
Г

60	A right rectangular prism has a length of $2\frac{1}{2}$ feet, a width of 3 feet, and a height
	of $1\frac{1}{2}$ feet. Unit cubes with side lengths of $\frac{1}{2}$ foot are added to completely fill
	the prism with no space remaining. What is the volume, in cubic feet, of the right
	rectangular prism?
	Show your work.
	$l \times w \times h = V$
	$2\frac{1}{2} \times 3 \times 1\frac{1}{2} = 11\frac{1}{4}$
	Or other valid process
	Answer cubic feet
	How many $\frac{1}{2}$ -foot unit cubes can be added to fill the prism completely? Use what
	you know about unit cubes or the side lengths of prisms to show your work or
	explain your answer.
	$1/_2 \times 1/_2 \times 1/_2 = 1/_8$
	$11\frac{1}{4} \div \frac{1}{8} = 11\frac{1}{4} \times 8 = 90$
	Or other valid process
	90 Answer unit cubes

1
A right rectangular prism has a length of $2\frac{1}{2}$ feet, a width of 3 feet, and a height
of $1\frac{1}{2}$ feet. Unit cubes with side lengths of $\frac{1}{2}$ foot are added to completely fill
the prism with no space remaining. What is the volume, in cubic feet, of the right
rectangular prism2 $V = / W H$
show your work. $V = \angle W H$ $V = 2\frac{1}{2} \cdot \frac{1}{2} \cdot \frac{3}{2}$ $V = 1/\frac{1}{4}$
v= ny
Answer $\frac{1}{4}$ cubic feet
How many $\frac{1}{2}$ -foot unit cubes can be added to fill the prism completely? Use what
you know about unit cubes or the side lengths of prisms to show your work or
explain your answer. $ \begin{aligned} & I  \frac{1}{y} - \frac{1}{y} - \frac{1}{y} - \frac{1}{y} - \frac{1}{y} - \frac{1}{y} + \frac{1}{y} - \frac{1}{y} - \frac{1}{y} + \frac{1}{y} - \frac{1}{y} - \frac{1}{y} + \frac{1}{y} - \frac{1}{y} + \frac{1}{y} + \frac{1}{y} - \frac{1}{y} + \frac{1}{y} + \frac{1}{y} - \frac{1}{y} + \frac{1}$
$11\frac{1}{4} = Volume of prism V = \frac{1}{8}$
Answer unit cubes

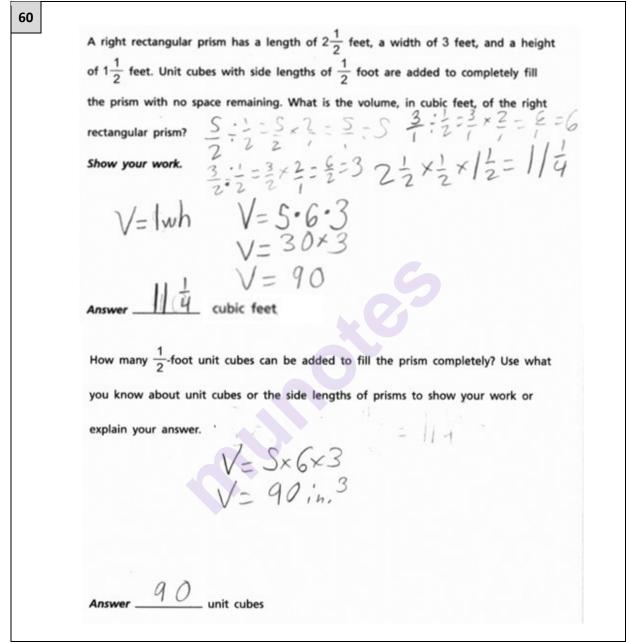
#### Score Point 3 (out of 3 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The volumes of the rectangular prism and the unit cube are correctly calculated. The volume of the rectangular prism is then divided by the volume of a unit cube to correctly solve for the number of unit cubes that will fit in the prism. This response indicates that the student has completed the task correctly, using mathematically sound procedures.



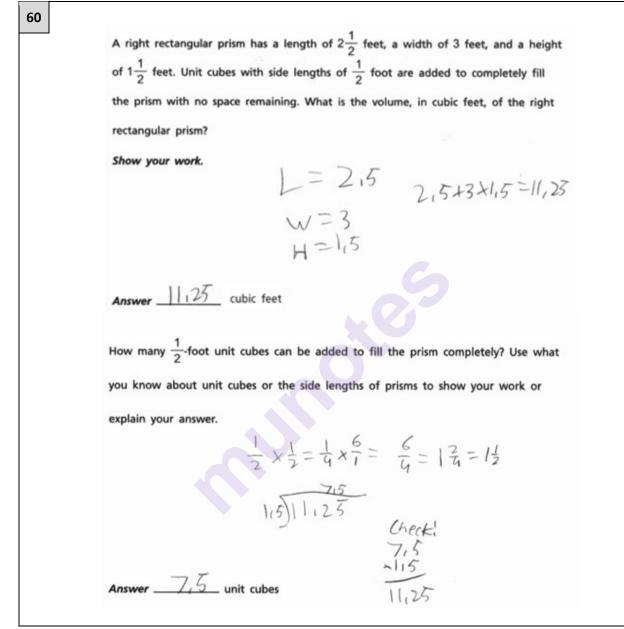
#### Score Point 3 (out of 3 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The volumes of the rectangular prism and the unit cube are correctly calculated. The volume of the rectangular prism is then divided by the volume of a unit cube to correctly solve for the number of unit cubes that will fit in the prism. This response is complete and correct.



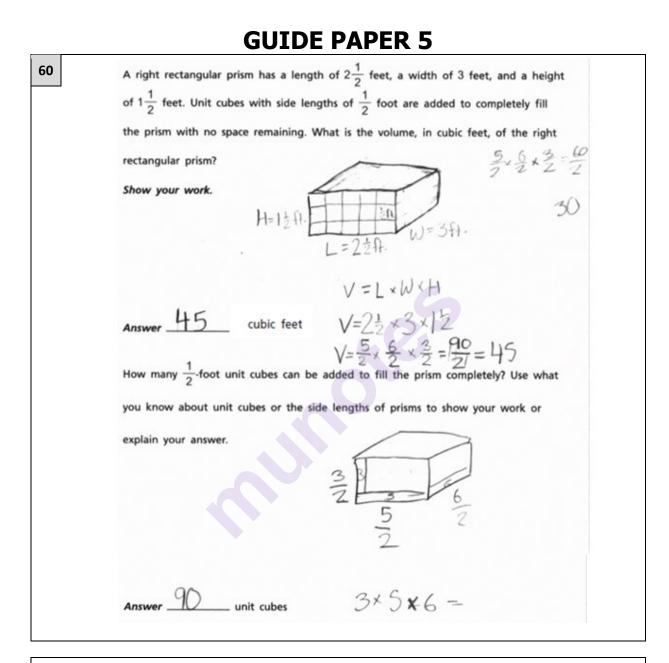
#### Score Point 3 (out of 3 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The volume of the rectangular prism is correctly calculated. The number of unit cubes that will fit along each side of the prism is calculated and then multiplied to determine the correct total number of unit cubes per prism.

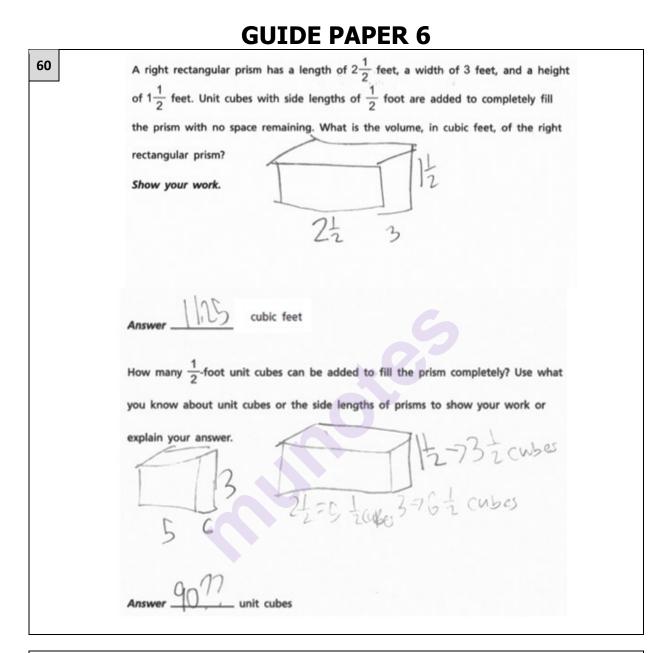


#### Score Point 2 (out of 3 points)

This response demonstrates a partial understanding of the mathematical concepts in the task. The volume of the rectangular prism is correctly calculated; however, the volume of a unit cube is not calculated correctly, the product of two side lengths is multiplied by 6 rather than by  $\frac{1}{2}$ . The number of unit cubes is correctly calculated using the incorrect volume of a unit cube. The response addresses most, but not all aspects of the task and reflects some minor misunderstanding of the underlying mathematical concepts.

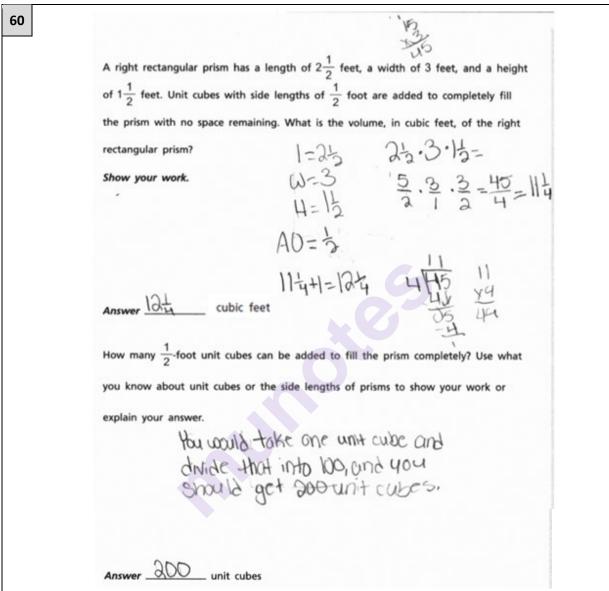


This response demonstrates a partial understanding of the mathematical concepts in the task. A correct procedure is followed to determine the volume of the rectangular prism ( $V = 2\frac{1}{2} \times 3 \times 1\frac{1}{2}$ ); however, a calculation error results in an incorrect solution. A diagram of the prism is used to count the number of unit cubes that will fit on each side of the prism and then those numbers are multiplied to determine the correct total number of unit cubes per prism. This response contains an incorrect solution but provides sound procedures.

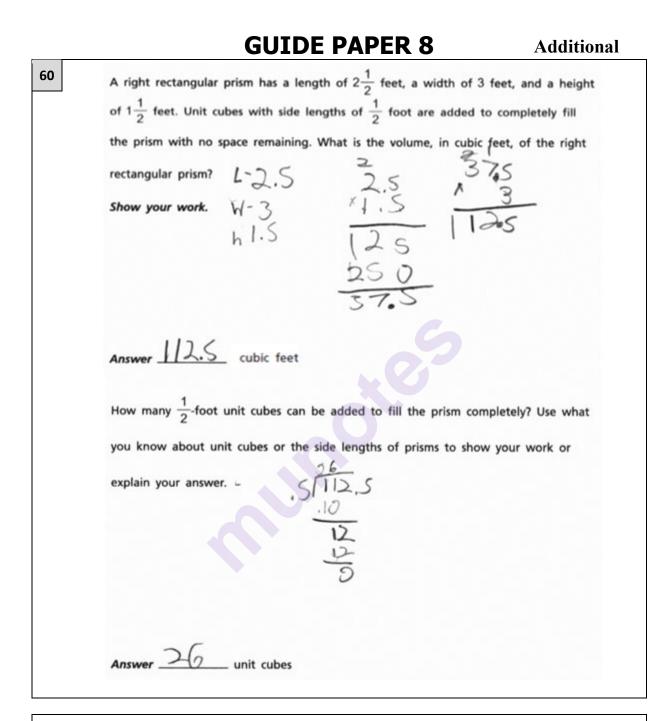


This response demonstrates a partial understanding of the mathematical concepts in the task. The volume of the rectangular prism is calculated correctly and a drawing of the rectangular prism with a label on each side is provided. Another diagram is provided and each side is labeled with a length of the prism and how many  $\frac{1}{2}$ -foot unit cubes will fit on each side of the rectangular prism  $(1^{1}/_{2} \rightarrow 3^{-1}/_{2} \text{ cubes}, 3 \rightarrow 6^{-1}/_{2} \text{ cubes}, 2^{1}/_{2} \rightarrow 5^{-1}/_{2} \text{ cubes})$ ; however, no additional operation is shown to support how the correct solution is obtained. The response appropriately addresses most, but not all aspects of the task.

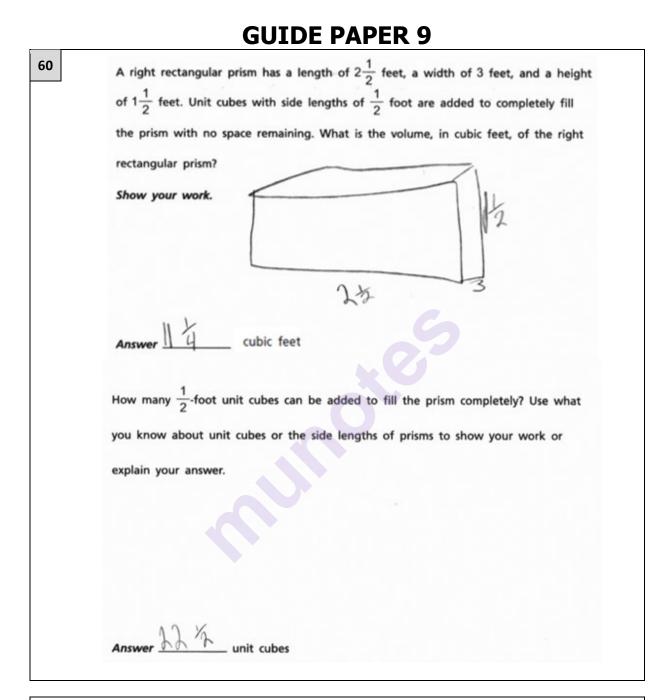




This response demonstrates only a limited understanding of the mathematical concepts in the task. The volume of the rectangular prism is correctly shown  $(2\frac{1}{2} \times 3 \times 1\frac{1}{2})$  and a correct solution of  $11\frac{1}{4}$  is calculated; however, an additional 1 is added to the answer resulting in an incorrect final solution of  $12\frac{1}{4}$ . The work shown for the number of unit cubes per prism is incorrect and incoherent. This response exhibits multiple flaws related to misunderstanding of important aspects of the task.



This response demonstrates only a limited understanding of the mathematical concepts in the task. The volume of the rectangular prism is correctly determined; however, the misplacement of the decimal point leads to an incorrect final solution for the volume of the prism. The volume of the prism is incorrectly divided by the length of one of the unit cubes sides. This response exhibits multiple flaws related to misunderstanding of important aspects of the task.



This response demonstrates only a limited understanding of the mathematical concepts in the task. The volume of the rectangular prism is calculated correctly and a drawing of the rectangular prism with a label on each side is provided; however, no operations are shown to support how the solution is obtained. This response contains the correct volume for the rectangular prism but required work is limited. The number of unit cubes per prism is incorrect and no work is provided.

	GUIDE PAPER 10
60	A right rectangular prism has a length of $2\frac{1}{2}$ feet, a width of 3 feet, and a height
	of $1\frac{1}{2}$ feet. Unit cubes with side lengths of $\frac{1}{2}$ foot are added to completely fill
	the prism with no space remaining. What is the volume, in cubic feet, of the right
	rectangular prism? $2 \pm + 1 \pm + 1 \pm - 3 \pm 3$
	rectangular prism? Show your work. $2\frac{1}{2} +  \frac{1}{2} + \frac{1}{2} = 3\frac{3}{2}$ $\frac{5}{2} + \frac{3}{2} + \frac{1}{2} = -\frac{9}{2} = 4\frac{1}{2}$
	Answer cubic feet
	How many $\frac{1}{2}$ -foot unit cubes can be added to fill the prism completely? Use what
	you know about unit cubes or the side lengths of prisms to show your work or
	explain your answer.
	3
	Answer unit cubes

All of the given dimensions are improperly added together; holistically this response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task.

	GUIDE PAPER 11	Additional
60	A right rectangular prism has a length of $2\frac{1}{2}$ feet, a width of 3 fe	eet, and a height
	of $1\frac{1}{2}$ feet. Unit cubes with side lengths of $\frac{1}{2}$ foot are added to	
	the prism with no space remaining. What is the volume, in cubic fe	et, of the right
	rectangular prism?	
	Show your work. $3 \times 5 = 4$	
	_	
	Answer $3\frac{3}{4}$ cubic feet $3\frac{3}{4}$	
	How many $\frac{1}{2}$ -foot unit cubes can be added to fill the prism complete	etely? Use what
	you know about unit cubes or the side lengths of prisms to show yo	our work or
	explain your answer.	
	15 + 2 = 15	
	=	
	7	
	Answer 1 8 unit cubes	

Although two of the given dimensions are properly multiplied, holistically this response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task.

The table below shows the elevations at which different artifacts were found during an 61 archeological dig. Artifact Elevation arrow head 15 feet above sea level bone 721 feet above sea level clay bowl sea level necklace 462 feet above sea level 1,200 feet below sea level woven basket Write the name of each artifact and the elevation at which each artifact was found using a positive integer, zero, or negative integer. Explain how you determined if an elevation required a positive integer, zero, or negative integer.

## **EXEMPLARY RESPONSE** The table below shows the elevations at which different artifacts were found during an 61 archeological dig. Artifact Elevation arrow head 15 feet above sea level bone 721 feet above sea level clay bowl sea level necklace 462 feet above sea level woven basket 1,200 feet below sea level Write the name of each artifact and the elevation at which each artifact was found using a positive integer, zero, or negative integer. arrow head = +15; bone = +721; clay bowl = 0; necklace = +462; woven basket = -1200 Or other valid response Explain how you determined if an elevation required a positive integer, zero, or negative integer. Artifacts found above sea level have a positive integer; artifacts found at sea level are zero; artifacts found below sea level have a negative integer. Or other valid response

		GUIDE F	PAPER 1	Additional
61	The table below she found during an ar		ns at which different a	artifacts were
		Artifact	Elevation	
		arrow head	15 feet above sea level	
		bone	721 feet above sea level	
		clay bowl	sea level	
		necklace	462 feet above sea level	
		woven basket	1,200 feet below sea level	

Write the name of each artifact and the elevation at which each artifact was found using a positive integer, zero, or negative integer.

Arrow head= 15 ft Bone=721 ft Clay bowl=0 ft Necklace=462 ft Woven basket= -1200 ft

Explain how you determined if an elevation required a positive integer, zero, or negative integer.

To find the answers to this problem you need to know that above sea level means that the numbers are postive so you dont add anything to the begining of the number. Below sea level means the number is negative so you put a negative sign in front of the number. At sea level means that you make the number zero because it is like the starting point and it isn't negative or positive.

## Score Point 3 (out of 3 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The artifacts are listed correctly with a positive integer for above sea level, zero for at sea level and a negative integer for below sea level with a correct explanation of how the student determined if the integers are positive or negative or zero. This response indicates that the student has used mathematically sound procedures.

## **GUIDE PAPER 2** The table below shows the elevations at which different artifacts were 61 found during an archeological dig. Artifact Elevation 15 feet above sea level arrow head bone 721 feet above sea level clay bowl sea level 462 feet above sea level necklace woven basket 1,200 feet below sea level Write the name of each artifact and the elevation at which each artifact was found using a positive integer, zero, or negative integer. -1,200, 0, +15, +462, +721 Explain how you determined if an elevation required a positive integer, zero, or negative integer. If a elevation requires a positive interger it has to say above sea level, for it to be zero it has to say sea level, and if it is a negative interger it has to say below sea level

## Score Point 3 (out of 3 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The elevations are listed correctly with a plus or negative sign as indicated and a zero for sea level. This response contains sufficient work to demonstrate a thorough understanding of the mathematical concepts.

## **GUIDE PAPER 3** The table below shows the elevations at which different artifacts were 61 found during an archeological dig. Artifact Elevation arrow head 15 feet above sea level bone 721 feet above sea level clay bowl sea level necklace 462 feet above sea level woven basket 1,200 feet below sea level Write the name of each artifact and the elevation at which each artifact was found using a positive integer, zero, or negative integer. Arrow Head: 15 ft Bone: 721 ft Clay Bowl: 0 ft Necklace: 462 ft Woven Basket: -1,200 ft Explain how you determined if an elevation required a positive integer, zero, or negative integer. I determined if an elevation required a positive integer, zero, or negative integer by looking at the elevation. If the elevation is below sea level it has a negative integer. If the elevation is

I determined if an elevation required a positive integer, zero, or negative integer by looking at the elevation. If the elevation is below sea level it has a negative integer. If the elevation is above sea level it has a positive integer. If the elevation is on sea level it has a zero for its elevation.

## Score Point 3 (out of 3 points)

This response demonstrates a thorough understanding of the mathematical concepts in the task. The artifacts are listed correctly with a positive integer for above sea level, zero for at sea level and a negative integer for below sea level with a correct explanation of how the student determined if the integers were positive, negative or zero. This response indicates that the student has used mathematically sound procedures.

## **GUIDE PAPER 4** The table below shows the elevations at which different artifacts were 61 found during an archeological dig. Artifact Elevation arrow head 15 feet above sea level bone 721 feet above sea level sea level clay bowl necklace 462 feet above sea level 1,200 feet below sea level woven basket Write the name of each artifact and the elevation at which each artifact was found using a positive integer, zero, or negative integer. arrow head +15 bone +721 clay bowl 0 necklace +462 woven basket -1,200 Explain how you determined if an elevation required a positive integer, zero, or negative integer. The words above , below or sea level

## Score Point 2 (out of 3 points)

This response demonstrates a partial understanding of the mathematical concepts in the task. The artifacts are listed correctly with a positive integer for above sea level, zero for at sea level and a negative integer for below sea level. The explanation is incomplete as to how the student determined if it was a positive, negative or zero integer. This response appropriately addresses most, but not all aspects of the task.

	Artifact	Elevation	
	arrow head	15 feet above sea level	
	bone	721 feet above sea level	
	clay bowl	sea level	
	necklace	462 feet above sea level	
	woven basket	1,200 feet below sea level	
	g a positive integer, <sup>ft.</sup> t.	d the elevation at which eac zero, or negative integer.	ch artifad
necklace:-462f woven basket:-			

This response demonstrates a partial understanding of the mathematical concepts in the task. All of the artifacts are listed correctly with the exception of the necklace, which should have a positive sign by the integer. The explanation provides sound reasoning on how the negative, positive and zero are determined. This response contains an incorrect solution but provides sound reasoning and explanation.

		PAPER 6		
	elow shows the elevation g an archeological dig	ons at which different arti	facts were	
	g an a an coord great ang	-		
	Artifact	Elevation		
	arrow head	15 feet above sea level		
	bone	721 feet above sea level		
	clay bowl	sea level		
	necklace	462 feet above sea level		
	woven basket	1,200 feet below sea level		
found using	a positive integer, zer	nd the elevation at which e o, or negative integer. wl 0 Feet Necklace 462 Feet Wow		
Feet				
•	v you determined if ar jative integer.	elevation required a pos	itive integer,	
Below Sea le	vel means a negative integ	er and above sea level means a	a positive intege	
	Score Point 2	2 (out of 3 points)		
-	emonstrates a partial un	derstanding of the mathema y with a positive integer for	-	

the task. The artifacts are listed correctly with a positive integer for above sea level, zero for at sea level and a negative integer for below sea level. The explanation is incomplete as it does not address the zero at sea level. This response appropriately addresses most, but not all aspects of the task.

	Artifact	Elevation	
	arrow head	15 feet above sea level	
	bone	721 feet above sea level	
	clay bowl	sea level	
	necklace	462 feet above sea level	
	woven basket	1,200 feet below sea level	
was found usir	ng a positive integer	d the elevation at which each , zero, or negative integer.	
	ou determined if an ive integer.	elevation required a positive i	nteg

This response demonstrates only a limited understanding of the mathematical concepts in the task. The artifacts are listed correctly with a positive integer for above sea level, zero for at sea level and a negative integer for below sea level; however, the explanation is missing. This response contains the correct solution but required work is limited.

## GUIDE PAPER 8 Additional The table below shows the elevations at which different artifacts were found during an 61 archeological dig. Artifact Elevation 15 feet above sea level arrow head 721 feet above sea level bone clay bowl sea level necklace 462 feet above sea level woven basket 1,200 feet below sea level Write the name of each artifact and the elevation at which each artifact was found using a positive integer, zero, or negative integer. CLAy bowl 0, arrow head -15, bone 721, necklace 462 Explain how you determined if an elevation required a positive integer, zero, or negative integer. if it was below sea leval it was a negative integer if it was above sea leval it was a positive integer.

## Score Point 1 (out of 3 points)

This response demonstrates only a limited understanding of the mathematical concepts in the task. The clay bowl, bone, and necklace artifacts are all listed correctly; however, the arrow head incorrectly has a negative sign and the woven basket is missing altogether. The explanation has correctly identified below as negative and above as positive; however, at sea level is not addressed. This response exhibits multiple flaws related to misunderstanding of important aspects of the task.

Artifact	Elevation
arrow head	15 feet above sea level
bone	721 feet above sea level
clay bowl	sea level
necklace	462 feet above sea level
woven basket	1,200 feet below sea level
a positive integer,	d the elevation at which each artizero, or negative integer.

This response demonstrates only a limited understanding of the mathematical concepts in the task. All of the artifacts are listed correctly with the exception of the necklace, which should have a positive sign by the integer. The explanation for how the zero is determined is correct; however, the explanation for how the positive or negative integers are determined is incomplete. This response addresses some elements of the task correctly but reaches an inadequate solution and provides reasoning that is incomplete.

		GUIDE F	PAPER 10	
61		v shows the elevation of the selevation of the s	ons at which different art	ifacts were
		Artifact	Elevation	
		arrow head	15 feet above sea level	
		bone	721 feet above sea level	
		clay bowl	sea level	
		necklace	462 feet above sea level	
		woven basket	1,200 feet below sea level	
			d the elevation at which , zero, or negative intege	
	0-0			
	Explain how yo zero, or negativ		elevation required a posit	ive integer,
	sea level			

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. The response is incoherent and incorrect.

	Artifact	Elevation	
	Artifact	Elevation	
	arrow head	15 feet above sea level 721 feet above sea level sea level 462 feet above sea level	
	bone		
	clay bowl		
	necklace		
	woven basket	1,200 feet below sea level	
found using	a positive integer, ze	nd the elevation at which e ro, or negative integer.	
Explain how	you determined if a ative integer.	n elevation required a pos	sitive intege
•	5		

This response is not sufficient to demonstrate even a limited understanding of the mathematical concepts in the task. The response only copies the chart from the prompt.