

ECE-102 / PECS141 - Elective-I : Information Theory And Coding

P. Pages : 2

Time : Three Hours



GUG/W/18/10982

Max. Marks : 70

- Notes : 1. Attempt **any five** questions.
2. Illustrate your answers wherever necessary with the help of neat sketches.

1. a) What is Shannon's theorem. List out the properties of codes using Shannon encoding algorithm. **6**
- b) Define Entropy. **8**
Consider a DMS w/m 8 possible symbols x_i where $L = 1, 2, 3, \dots, 8$ and their corresponding probabilities are
 $P(x_1) = 0.36$
 $P(x_2) = 0.25$
 $P(x_3) = 0.12$
 $P(x_4) = 0.10$
 $P(x_5) = 0.05$
 $P(x_6) = 0.08$
 $P(x_7) = 0.03$
 $P(x_8) = 0.01$
Find entropy of source and efficiency of code.
2. a) Derive the expression for channel capacity. **7**
- b) Explain source coding and channel coding. Explain the difference between them. **7**
3. a) Explain Lempel - Ziv encoding algorithm with suitable example. **7**
- b) Apply Huffman coding algorithm for the following messages - **7**
 $[X] = [X_1 \ X_2 \ X_3 \ X_4 \ X_5 \ X_6 \ X_7]$
 $[P] = [Y_2 \ Y_4 \ Y_4 \ Y_8 \ Y_8 \ Y_{16} \ Y_{16}]$
Suppose $M = 2$ then find -
i) Average length of codeword
ii) Entropy
iii) Efficiency of code
4. a) Calculate the syndrome vector of a single bit error if the parity check matrix of (7, 4) **8**
Hamming code is given as -
$$H = \left[\begin{array}{cccc|ccc} 1 & 1 & 1 & 0 & 1 & 0 & 0 \\ 0 & 1 & 1 & 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 & 0 & 0 & 1 \end{array} \right]$$

Find all the code vectors and find the error syndrome if there is error in the 3rd bit of the 4th code in the code sequence.

- b) What is the role of inter leaving in the performance of concatenated codes. How is it used to improve the performance of these codes ? 6
5. a) Discuss the role of $d_{\min}$ in error correction and detection methods. 7
- b) Describe Viterbi decoding algorithm. 7
6. a) For a (2, 1, 3) convolution code described by $g_1 = [1\ 0\ 1]$ and $g_2 = [1\ 1\ 0]$ draw the state diagram, tree diagram and Trellis diagram. 8
- b) Differentiate between convolution codes and block codes. 6
7. a) Explain iterative coding using in BCJR algorithm. 8
- b) Discuss upper and lower bounds in linear codes. 6
8. Write short notes on **any two**. 14
- a) Justeen codes.
- b) Reed Solomon codes
- c) Turbo codes
