## **University of Mumbai**

## **Examinations Summer**

Program No: 1T01034

Name of the Examination : S.E.(Electronics and Telecommunication )(SEM-IV)(Choice Base Credit Grading System ) (R- 19) (C Scheme)
Subject (Paper Code): 40821 / / Engineering Mathematics-IV

Time: 2 hour 30 minutes Max. Marks: 80

## NB:

1. All the questions are COMPULSORY.

2. Write the correct option for multiple choice question (MCQ) in Q. 1

**3.** Q.2 to Q. 4 have internal choice within question.

4. Figures to the right indicate full marks.

**5.** Use of scientific calculator is allowed.

Q1. (20 Marks)	Choose the correct option for following questions. All the Questions are compulsory and carry equal marks  2marks each							
1.	The function $f(z) = \frac{2}{(z+5)^3(z-2)^4}$ has poles at z=-5 of order and z=2 of order							
Option A:								
Option B:	3,4							
Option C:	2,4							
Option D:								
2.	If f(z) is analytic function and f'(z) is continuous at all points inside and on simple closed curve 'C', then							
Option A:	$ \oint_C f(z)dz = 0 $							
Option B:	$\oint_C f(z)dz \neq 0$							

0 0	
Option C:	
	$\oint_C f(z)dz = 2\pi i f(a)$
Option D:	
option B.	$\oint f(z)dz = 1$
	$\phi f(z)dz = 1$
3.	The rank of the matrix A is the
Option A:	Dimension of the row space A
Option B:	Dimension of the column space A
Option C:	Both option A and B
Option D:	Dimension of the null space of A and B
4.	Let $Q(X) = X^T A X$ , be a quadratic form in 'n' variables then which
4.	
	of the following statement is wrong
Option A:	The total number of non-zero terms in the canonical form of
	quadratic form is called as rank of quadratic form
Option B:	The number of positive square terms in the canonical form is called
	as Index of the quadratic form
Option C:	The difference between number of positive and negative terms in
1	the canonical form is called as signature of the quadratic form
Option D:	Signature of the quadratic form is greater than rank of quadratic
Option D.	form
5	The necessary condition for $\int_{x_1}^{x_2} f(x, y, y') dx$ to be maximum or
	minimum is
Option A:	at a cat
Option 71.	$\left  \frac{\partial f}{\partial y} - \frac{d}{dx} \left( \frac{\partial f}{\partial y'} \right) \right  = 0$
Option B:	$\partial f = d \cdot \partial f \cdot $
	$\left  \frac{\partial}{\partial y} + \frac{\partial}{\partial x} \left( \frac{\partial}{\partial y'} \right) \right  = 0$
Option C:	$\partial f = d / \partial f $
Option C.	
16 6 7 J J J J J	$\partial y' = dx (\partial y)$
Option D:	$\left  \frac{\partial f}{\partial x} + \frac{d}{\partial x} \left( \frac{\partial f}{\partial x} \right) \right  = 0$
	$\left(\frac{\partial y'}{\partial y'} + \frac{\partial x}{\partial x} \left(\frac{\partial y'}{\partial y'}\right) - 0\right)$
6 6 6 6 7 N N N	
6.	If the vectors [k, k, -2] and [k, -2, 12] are orthogonal vectors, then
	0.0/LV.6/AV
17 0 (6° 6°)	the values of 'k' are

Option A:	k = 6 or	· k = -	-4			(D) (S) (S) (S) (S)	6 6 9 0 V V V				
Option B:	k = 6 or										
Option C:	k = 3 or										
Option D:	k = 2  or				1999						
1	_				7000	50000000000000000000000000000000000000					
7.	The value	e of coef	ficient of	f correlation	on lies bet	ween					
Option A:	0 to 1	The value of coefficient of correlation lies between 0 to 1									
Option B:	-∞ <i>to</i> 1			00,000		9 6 6 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7					
Option C:	0 to ∞			DX 3900	6666	7 16 6 7 F.					
Option D:	-1 to 1										
			,5)	20 25 CO	50 × 30 00 00 00 00 00 00 00 00 00 00 00 00		16 5 7 7 7 7 6 7 6 P				
8.	The rank correlation coefficients of the following data is										
	X	23	25	27	29	31	33				
	Y	43	45	47	49	51	53				
Option A:	0	\$ P. P.									
Option B:	-1										
Option C:	1	N 15 00 6	30 90 90 40 10	7, 10,6,7		\$2000 C					
Option D:	0.99										
	200		12 13 16 16 15 15 15 15 15 15 15 15 15 15 15 15 15		16 4 A A A						
9.	If 'X' and 'Y' are two normal variables with mean 40 and 50 with standard deviation 4 and 3 respectively, what is the distribution of X+Y										
Option A:	N(90, 7)	0,000									
Option B:	N(90,3)			825000	10 %.						
Option C:	N(90, 5)		100 B		V						
Option D:	N(90,4)		7000	8,63,53							
39,500		STATE OF THE	5 6 6 7 A 6	10000							
10.	the first s	uccess in	n an infir	. 77	of indepen	ndent trials	preceding with the				
Option A:	$\frac{p}{q}$		00 00 00 00 00 00 00 00 00 00 00 00 00								
Option B:	$\frac{q}{p}$	23 45 75 19. 25 72 19. 25.	Shr								
Option C:	$\frac{p+1}{q}$										
Option D:	$\frac{p^2}{q^2}$	5.00 A									

Q2 (20 Marks)	Solve any Four out of Six									5 marks each			
A	Find the extremals of the functional $\int_0^1 \{y'^2 + 12xy\} dx$ subject to $y(0) = 0$ and $y(1) = 1$												
В	For real values of a, b and $\theta$ , using Cauchy- Schwarz inequality, show that $(a\cos\theta + h\sin\theta)^2 < a^2 + h^2$												
C	Evaluate $\oint_C \frac{\sin^6 z}{\left(z - \frac{\pi}{6}\right)^3} dz$ where C is the circle $ z  = 1$												
D	Find the probability that at most 4 defective bulbs will be found in a box of 200 bulbs, if it is known that 25 of the bulbs are defective.												
	Ten students got the following percentage of marks in mathematics and statistics												
Е	Maths	78	36	98	25	75	82	90	62	65	39		
	Stats	84	51	91	60	68	62	86	58	53	47		
F	twice as many times as B, and machines B and C produce equal number of items . 3% of bolts produced by A and B are defective and 5% of bolts produced by C are defective . All bolts are put into one stock pile and one is chosen from this pile. What is the probability that it is defective?												
Q. 3 (20 Marks)	Solve any Four out of Six 5 marks each												
À	Test for an extremal of the functional $\int_0^1 \{xy + y^2 - 2y^2y'\} dx$ with $y(0)=0$ , $y(1)=2$												
B	Show that the set $W = \{[x, y, z]   y = x + z\}$ is a subspace of $R^3$ under usual addition and scalar multiplication.												
C	6 5 7 7 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	e stra	ight l	ine fro	om z=	0 to z=	0 <b>:1+i</b>	- y + iz		along paralle	el to the		

	i	magina	iry axis f	rom z=1	to z=1-	+i					
D	Reduce the matrix of the quadratic form $6x_1^2 + 3x_2^2 + 3x_3^2 - 4x_1x_2 + 4x_1x_3 - 2x_2x_3$ to canonical form by congruent transformation and find rank, signature, value class.										
E	Obtain the equations of the lines of regression for the following data.										
	X	65	66	67	67	68	69	70	72		
	Υ	67	68	65	68	72	72	69	71		
	A rand	dom va	riable X	has the	followii	ng prob	ability d	istributi	on-		
		Χ	-2	-1,80	0		2	3	X \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \		
F		Р	0.1	K	0.1	2K	0.2	3K			
	(i) Find	(i) Find the constant K. (ii) Find the mean and variance of X.									
Q. 4 (20 Marks)	Solve any Four out of Six 5 marks each										
A	Using Rayleigh-Ritz method, find an approximate solution for the extremal of the functional $\int_0^1 \left\{ xy + \frac{1}{2}y'^2 \right\} dx$ subject to $y(0)=y(1)=0$										
В	Using Gram-Schmidt process, construct an orthonormal basis for the plane x+y+z=0										
C	Obtain Taylor's and Laurent's series expansions of $f(z) = \frac{2}{(z-1)(z-2)}$ When 1										
D	Find Singular value decomposition of $\begin{bmatrix} 2 & 2 \\ -1 & 1 \end{bmatrix}$										
	Fit a straight line of the form y=a+bx to the following data										
Ě	33,50	X		3.0	5	7	8	10	)		
1000	2238	Y	8	12	15	17	18	20	)		
F	A rand	dom va	fiable $x$ $f(x)$	has proba $= \begin{cases} kx^2e \\ 0 \end{cases}$	ability d $e^{-x}$	lensity f $x > 0$ ,	unction $k > 1$	0			
STATE OF THE STATE	Find (	d and h	ence fin	d mean	and var	<i>Uti</i> riance	nerwise	?			