

Duration: 3 Hours

Marks:80

Note:

1. Q.no. 1 is compulsory.
2. Answer any three questions from Q. No. 2 to Q. No. 6.
3. Write in legible handwriting.
4. Make any suitable assumptions wherever required.
5. Must make suitable supporting diagrams wherever desired.
6. Figure to the right indicates marks.

- Q1 Each question carries five marks 20
- a. Why is the phase margin increased above that desired when designing a lead compensator?
 - b. Define observability. Explain how it can be determined for a controller canonical representation.
 - c. Why is there less improvement in steady-state error if a lag controller is used instead of a PI controller?
 - d. The horizontal lines on the s-plane are lines of constant peak time. How these points can be mapped to z-plane? Justify with the equation.
- Q2 a. Given the unity feedback system with $G(s) = \frac{K}{(s+4)(s+6)(s+12)}$ use Root locus technique to determine the value of gain K to yield a step response with a 15% overshoot. 10
- b. Given the following open loop plant $G(s) = \frac{10}{s(s+2)(s+4)}$. Design a controller to yield a 15% overshoot and a peak time of 0.4 sec assuming that the plant is represented in the phase variables form. Assume third pole 10 times farther from the imaginary axis than the dominant poles. 10
- Q3 a. For the digital system with forward transfer function $G(z) = \frac{0.56}{(z-2)(z-3)(z-0.5)}$ find the static error constants and the steady state error if the inputs are $u(t)$, $t u(t)$ and $\frac{t^2}{2} u(t)$. Sampling time $T=0.1$. 10
- b. For a unity feedback system with $G(s) = \frac{K}{(s+2)(s+6)(s+8)}$ design a lag compensator using bode plot so that the system operates with a 10% overshoot and a static error constant of 100. 10
- Q4 a. Consider the plant $G(s) = \frac{20}{(s+5)(s+6)(s+9)}$ which is represented in parallel form. Design an observer with a transient response described by $\zeta=0.45$ and $\omega_n=100$. Place the observer third pole 10 times as far from the imaginary axis as the observer dominant poles. Transform the plant to observer canonical form for the design. Then transform the design back to parallel form. 15

- b. Find $G(z)$ for $G(s) = \frac{20}{(s+5)}$ in cascade with a sampler and a zero-order sample and hold. The sampling period is 0.25. 05
- Q5 a. A unity feedback system with forward path transfer function $G(s) = \frac{K}{s(s+5)(s+8)}$ has 15% overshoot. Evaluate the current dominant poles using R.L and then design a PD controller to reduce the settling time by a factor of 2. 10
- b. Given a sampler and z.o.h. in cascade with $G(s) = \frac{3}{(s+3)}$ find the range of T to make the system stable. 10
- Q6 a. Given the plant $\dot{x} = \begin{bmatrix} 2 & 1 \\ 0 & 1 \end{bmatrix} x + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u; \quad y = [1 \quad 1] x$ 10
- Design an integral controller to yield a 12% overshoot, 2 sec. settling time and zero steady state error for a step input.
- b. Compare lag and lead compensator with respect to application, pole-zero plot and circuit for implementation. Construct the transfer functions of lag and lead compensators from their respective circuits. 10