(Time: 3 hours) [Total marks 100]

Note: 1. All questions are compulsory.

- 2. Figure to the right indicates full marks.
- 3. Use of calculator is permitted.
- Q.1. (a) (i) Define the term force of mortality (μ_x) . By making suitable assumptions prove that $\mu_x = \frac{(l_{x-1} l_{x+1})}{2 \, l_x}$
 - (ii) Define central death rate (m_x) . Show that $p_x = \frac{2 m_x}{2 + m_x}$ (04)
 - (b) (i) Define the term curate expectation of life (e_x) and complete expectation of life (e_x^0) . Further in usual notations, show that –

 (1) $e_x = \frac{\sum_{i=1}^{\infty} l_{x+i}}{l_x}$ (2) $e_x^0 = \frac{1}{2} + e_x$
 - (ii) If $l_x = 100 \sqrt{100 x}$ then find probability of person with age 10 years will survive 5 more years.

OR

(02)

- (p) (i) State and prove Makeham's first law of mortality. (06)
 - (ii) Explain the following terms-
 - (1) Select mortality.
 - (2) Aggregate mortality.
- (q) Prove that- The average age at death of those who die in the age group x to x + n is given by, $x + \frac{T_x T_{x+n} nl_{x+n}}{l_x l_{x+n}}$ (10)
- Q.2. (a) Define nominal rate of interest (i^(m)) and effective rate of interest (i). (10) Further in usual notations, show that $i^{(m)} = m \left[\sqrt[m]{(1+i)} 1 \right]$
 - (b) Obtain an expression for present value and accumulated value of immediate annuity of Rs. 1 p.a. when successive payments are in Arithmetic progression. (Assume rate of interest is i per unit per annum)

OR

- (p) (i) Obtain an expression for present value of deferred immediate annuity certain and in usual notations show that $a_{m+n|}$ $a_{m|} = m|a_{n|}$ where m is deferment period. (Assume rate of interest is i per unit per annum)
 - (ii) In usual notations show that $-\frac{a_{6nl}}{a_{3nl}} = 1 + v^{3n}$ (03)

	(q)	Define the following terms- (i) perpetuity (ii) Immediate perpetuity (iii) perpetuity due Hence obtain expression for present value of deferred perpetuity due and deferred immediate perpetuity of Rs.1 p.a. with deferment period of m years. (Assume rate of interest is i per unit per annum)	(10)
Q.3.	(a)	Define Deferred immediate life annuity. Obtain the expression for the present value of deferred immediate life annuity of Rs. 1 p.a. to a person aged x in terms of commutation functions.	(10)
	(b)	Define life annuity due. Obtain the expression for present value of life annuity due of Rs. 1 p.a. on a life now aged x for 'n' years in terms of commutation functions. OR	(10)
	(p)	Define the term temporary life annuity. How is it different form annuity certain? Obtain the expression for the present value of immediate temporary life annuity of Rs. 1 p.a. to a person aged x years in terms of commutation functions.	(10)
	(q)	Obtain the expression for the present value of increasing life annuity when the payments are made at the end of each year to a person aged x. Write the result in terms of commutation functions.	(10)
Q.4.	(a)	Obtain the expression for the level annual premium for temporary assurance in terms of commutation functions after deriving all the necessary results.	(10)
ST STATE OF THE ST	(b)	Compute the present value of Pure endowment assurance plan. Derive it's the level annual premium in terms of commutation functions. OR	(10)
	(p)	Obtain the present value of special endowment assurance plan. Derive the expression for level annual premium in terms of commutation functions for this plan.	(10)
	(q)	Derive the expression for the level annual premium for whole life assurance in terms of commutation functions after deriving all the necessary results.	(10)

- **Q.5.** Attempt **ANY TWO** sub-questions.
 - (a) (i) Prove that-Probability that among three live all aged x years, the first (06) death will occur in $(t+1)^{th}$ year is given by $(t P x)^3$ $(t+1 P x)^3$
 - (ii) State uses of life tables. (04)
 - (b) Obtain an expression for accumulated value of immediate annuity of Rs. 1 p.a. payable p times a year for n years certain. (Assume rate of interest is i per unit per annum)
 - (c) Derive the expression for the present value of deferred life annuity due of Rs. 1 p.a. payable to a person aged x in terms of commutation functions.
 - (d) Explain the concept of limited payment assurance with the help of endowment assurance plan. Derive the level annual premium for the same in terms of commutation functions.