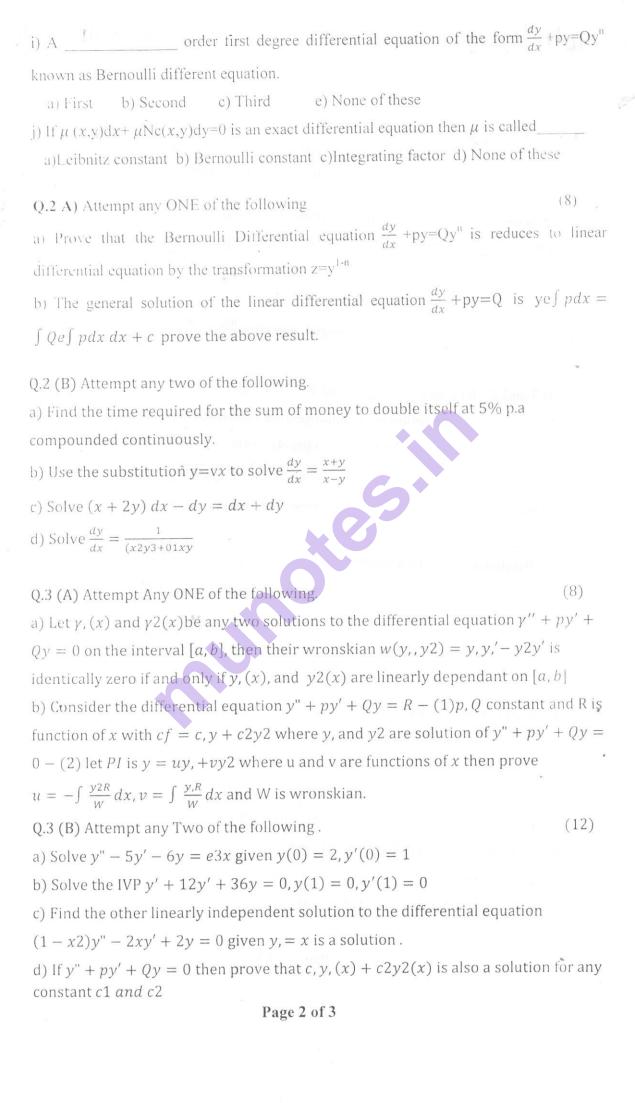
## VCD 10 10 19 SYBSC(PM) (ATKT) SEM-IV(Choice Based) MATHS- III Marks: 100 3 Hours

Instructions: 1) All questions are compulsory.

2) All questions carry equal marks.  3) Figures to right Indicate full marks of subquestion.
Q.1 Choose correct alternative in each of the following. (20)
a) If n= then the Bernoulli differential equation reduce to variable separable
form.
i) 0 ii) 1 iii) 2 iv) None of these
b) The order and degree of differential equation $\frac{d3y}{dx^3} - \frac{d2}{dx^2} + 2\frac{dy}{dx} - 3y = \cos x - 1$ is
i) 3 and 2 ii) 2 and 3 iii) 3 and 1 iv) 1 and 3
of the following is homogenous differential equation.
i) $(x+y)dy + (5x-3y+8)dx=0$ ii) $(6x-4y+3)dx=(3x-2y+1)dy$
iii) $(2x+y-3)dy = (x+2y-3)dx$ iv) $x3dy=(y^3+y^2)\sqrt{y^2-x^2}dx$
d) Orthogonal trajectories of the family of curves xy=k represents a family of
a) Parabolas b) Straight lines c) Hyper bolas d) Circles
a) Parabolas b) Straight lines c) Hyper bolasti) Cheles
e) If $(e^{4t}, e^{4t})$ and $(e^{-2t}, -e^{-2t})$ are linearly independent solutions of $\frac{dx}{dt} = x + 3y$ , $\frac{dy}{dt} = 3x + y$
then Particular solution for which $x(0)=5$ , $y(0)=1$ is
a) $(3e^{4t}+2e^{4t}, 3e^{-2t}-2e^{-2t})$ b) $(4e^{4t}+e^{4t}, 4e^{-2t}-3e^{-2t})$
c) $(3e^{4t}+2e^{-2t}, -2e^{-4t}+e^{-2t})$ d) $(3e^{4t}+2e^{2t}, 3e^{4t}-2e^{-2t})$
f) The equation $D2 + PD + Q = 0$ is called
a) Auxiliary equation b) Characteristic equation
c) both a & b d) None of these
g) If $y_1 = x^2 1 x 1$ and $y_2 = x^3$ , $x \in 1R$ then Wcy . $_1y_2$ ) is
a) 0 b) 1 c) -1 d) None of these
h) The general solution of 2y"+5y'-12y=0 is
a) $y=c,e^{3x}+c2e^{4x}$ b) $y=c,e^{-3x}+c2e^{-4x}$
b) $y=c,e^{-4}x+c2e^{3}x^{12}$ d) None of these



Q.4 (A) Attempt any ONE of the following.

(8)

a) If w(t) wronskian of two solutions x = x, (t)y = y, (t) and x = x2(t), y = y2(t) to the homogeneous linear system  $\frac{dx}{dt} = a$ , (t)x + b, (t)y,  $\frac{dy}{dt} = a$ , (t)x + b2(t)y then prove either w(t) is identically equal to zero or w(t) is never zero on [a, b] b) If the auxiliary equation to the homogeneous system of equation with constant

b) If the auxiliary equation to the homogeneous system of equation with constant coefficients  $\frac{dx}{dt} = a, x + b, y, \frac{dy}{dt} = a2x + b2y$  (1)

has real equal roots m,m then there exist non trivial constant  $A_1, B_1, A_2, b_2, A_3, B_3$  such that  $x = A, e^{\text{mt}}.y = B, e^{\text{mt}}$  and  $x = (A2 + A3t)e^{\text{mt}}.y = (B2 + B3t)e^{\text{mt}}$  are linearly independent solutions to the system (1)

Q.4(B) Attempt any Two of the following

(12)

- a) show that x = 3t 2, y = -2t + 3 is particular solution to the non homogeneous system  $\frac{dx}{dt} = x + 2y + t 1$ ,  $\frac{dy}{dt} = 3x + 2y 5t 2$
- b) Find the third order differential equation whose equivalent system of linear equation is  $\frac{dx_1}{dt} = x2 \frac{dx_2}{dt} = x3, \frac{dx_3}{dt} = -\frac{8}{t}x3 + \frac{16}{t^2}x2 \frac{5}{t^3}x1$
- c) Find the general solutions to the system  $\frac{dx}{dt} = 4x 3y$ ,  $\frac{dy}{dt} 8x 6y$
- d) Prove that x = 3t + 2, y = 2t 1 is a particular solution to the non-homogeneous linear system.

Q.5 Actempt any Four of the following

(20)

- a) Find the general solution to the given system  $\frac{dx}{dt} = x 4y$ ,  $\frac{dy}{dt} = x + y$
- b) Find the general solution to the system satisfying initial conditions  $\frac{dx}{dt} = x + \frac{dx}{dt}$

$$y, \frac{dy}{dt} = y \text{ with } x(0) = -3, y(0) = 3$$

- c) solve  $y'' + 3y' + 2y = sine^x$
- d) Solve the IVP for  $\frac{d2y}{dx^2} 4\frac{dy}{dx} 12y = 3e^{5x}$  with  $y(0) = \frac{18}{7}$  and  $y'(0) = -\frac{1}{7}$
- e) Solve  $x \frac{dy}{dx} = 4 2y$  with initial condition y(1) = 0
- f) If  $(x + y)^n$  is an integrating factor of  $94x^2 + 2x + 6y$ )  $dx + (2x^2 + 9y + 3x) = 0$  then find n and solve the equation.