

Note : 1) Figures to Right indicates full marks.

2) All questions are Compulsory.

84-4

Q. 1 Solve any two

10

- 1) Using bisection method find the root of $x^2 - \log x - 12$ in the interval $[3, 4]$
- 2) Solve the equation $x^3 - 20$ by taking initial root $x_0 = 2$ by using Newton-Rapshon method.
- 3) Given $f(1) = 7$ $f(2) = 18$ $f(3) = 35$ $f(4) = 38$ find $f(2.5)$ by Lagranges interpolation.
- 4) Using Newton interpolation formula find $f(1.7)$ from the table

| | | | | | |
|--------|----|----|----|-----|-----|
| x | -2 | -1 | 0 | 1 | 2 |
| $f(x)$ | 4 | 26 | 58 | 112 | 466 |

Q. 2 Solve any two

10

- 1) Use Gauss Jordon method to solve system of equation if $2x + y + 6z = 9$; $8x + 3y + 2z = 13$, $x + 5y + z = 7$
- 2) Solve the given system of equation of Gauss Seidal Method $10x + y + z = 12$;
 $2x + 10y + z = 13$, $2x + 2y + 10z = 15$
- 3) Given that $\frac{dy}{dx} = 2 + \sqrt{xy}$ $y(1) = 1$ find y at $x = 2$ in step of 0.2 using Euler's Modified Method.
- 4) Using R - K 4th order find y at $x = 1.2$ if $\frac{dy}{dx} = x^2 + y^2$ $y(1) = 1.5$ taking $h = 0.1$

Q. 3 Solve any two

10

- 1) Find regression equation y on x and x on y , regressiion cofficient with the help of given data.

| | | | | | | | |
|-----|---|---|---|---|---|---|---|
| x | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| y | 1 | 5 | 3 | 6 | 4 | 8 | 9 |

- 2) Fit a second degree of Parabola by least squre method with the help of given data

| | | | | | |
|-----|---|---|---|----|----|
| x | 1 | 2 | 3 | 4 | 5 |
| y | 3 | 7 | 9 | 11 | 14 |

- 3) Ten students got the following marks in Mathematics & Java

| | | | | | | | | | | |
|-------------------|----|----|----|----|----|----|----|----|----|----|
| Student (Roll no) | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| Marks in Maths | 78 | 36 | 98 | 25 | 25 | 82 | 90 | 90 | 65 | 65 |
| Marks in Java | 84 | 51 | 91 | 60 | 68 | 62 | 86 | 58 | 53 | 47 |

Calculate Rank by Spearman.

- 4) Find Karl Pearson's coefficient of correlation from data if $n = 10$ $\sum(x - 43)^2 = 1712$ $\sum x = 430$
 $\sum y = 145$ $\sum(y - 14)^2 = 85$ $\sum(x - 43)(y - 14) = 353$

Q. 4 Solve any two

- 1) Define Binomial, poisson and normal distribution and give the difference between Binomial & normal with their properties.
- 2) Calculate first four central moments, β_1, β_2 if

| | | | | | |
|-----|---|---|---|---|---|
| x | 2 | 3 | 4 | 5 | 6 |
| f | 1 | 3 | 7 | 3 | 1 |

- 3) The mean and variance of a binomial distribution are 3 and 2 find probability that variate takes place i) less than or equal to two ii) greater than equal to seven. Also find S.D., Kurtosis, Skewness.
- 4) One fifth percent of the blades produced by a blade manufacturing factory turn out of defective the blades are supplied in packets of 10 use poisson distribution to find approximate number of packets containing 1) no defective 2) one defective 3) two defective 4) mean, variance, skewness and kurtosis.

Q. 5 Solve any two

- 1) The number of bike accidents per month in a city was found as below 20, 17, 12, 6, 7, 15, 8, 5, 16 and 14 test goodness of fit (Given that χ^2 at 5% is 19.02, $v = 9$)
- 2) Define Chi-square test with properties and uses
- 3) The certain drug is claimed to be effective in curing colds In an experiment on 164 people with cold, half of given drug and half of them given sugar pills the patients reactions to the treatment are recorded in following table test the hypothesis that the drug is not better than sugar pills for curing cold.

| | | | | |
|------------------|--------|--------|-----------|-------|
| | Helped | Harmed | No effect | Total |
| Drug given | 52 | 10 | 20 | 82 |
| Sugar pill given | 44 | 12 | 26 | 82 |
| Total | 96 | 22 | 46 | 164 |

(Given that when $V = 2$ χ^2 at 5% = 5.99)

- 4) Solve the following LPP by Simplex Method $\text{Min } z = x_1 - 3x_2 + 2x_3$
 Subject to $3x_1 - x_2 + 2x_3 \leq 7$; $-2x_1 + 4x_3 \leq 12$
 $-4x_1 + 3x_2 + 8x_3 \leq 10$ $x_1, x_2, x_3 \geq 0$

Q. 6 Solve the following (any two)

216

10

- 1) Define i) Test of hypothesis ii) level of significance A die was thrown 9000 times and a throw of 5 or 6 was obtained 3240 times on the assumption of random throwing do the data indicates an unbiased die?
- 2) A random sample of size 16 has 53 mean the sum of the square of the deviation taken from the mean is 150 can this sample be regarded as taken the population having 56 mean obtain 95% and 99% confidence limits of mean population
[Given - $V = 15$ t at 1% 2.95 $V = 15$ t at 5% 2.13]

- 3) A test given two groups of students the marks obtained are as -

| | | | | | | | | | |
|-----------------------|----|----|----|----|----|----|----|----|----|
| 1 st group | 18 | 20 | 36 | 50 | 49 | 36 | 34 | 49 | 41 |
| 2 nd group | 29 | 28 | 26 | 35 | 30 | 44 | 46 | 46 | 38 |

Check the significance of difference between marks obtained the students of two group
(Given $V = 14$ t at 5% is 2.14)

- 4) Define student t - distribution with properties.

Q. 7 Solve any three

15

- 1) Find the root of equation by false position upto four iteration if $f(x) = x^3 + 3x^2 - 7$
- 2) Find $\int_1^4 (4x + 1) dx$ using Simpson's $\frac{1}{3}$ rd and $\frac{3}{8}$ th rule using six interval.

- 3) Find the equation of line by least square method with the help of given data

| | | | | | | | |
|-----|-----|-----|-----|-----|-----|-----|-----|
| x | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| y | 1.1 | 1.3 | 1.5 | 1.7 | 1.9 | 2.1 | 2.3 |

- 4) In an experiment on immunization of cattle from T.B. the following table are obtained.

| | | | |
|----------------|--------|------------|-------|
| | Affect | Non-Affect | Total |
| Inoculated | 12 | 26 | 38 |
| Non-Inoculated | 16 | 06 | 22 |
| Total | 28 | 32 | 60 |

(Given $V = 1$ η^2 at 5% is 3.84)

- 5) The following data pertain to two types of tube-bulbs tested for their length of life

| Type | Sample size | Mean | Variance |
|---------|-------------|------|----------|
| Type-I | 5 | 550 | 100 |
| Type-II | 7 | 500 | 81 |

test whether there is significant difference between two means at 5% level.

- 6) A random variable x has following probability

| | | | | | | | | |
|---------------|---|------|------|-----|------|-------|--------|----------|
| Values of x | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| $p(x)$ | 0 | $2k$ | $3k$ | k | $2k$ | k^2 | $7k^2$ | $2k^2+k$ |

find i) k ii) $P(x < 6)$ iii) $P(x \geq 6)$

— The End —