

Sub: - Mathematics & Statistics.

Note: 1) All questions are compulsory and carry equal marks.

2) Use of simple calculator is allowed

3) Figures to right indicate full marks.

SECTION - I

1) a) Calculate Karl Pearson's coefficient of correlation for the following data:

|   |    |   |    |    |    |    |
|---|----|---|----|----|----|----|
| x | 17 | 8 | 12 | 13 | 10 | 12 |
| y | 13 | 7 | 10 | 11 | 8  | 9  |

b) Find five yearly moving average (C)

|             |      |      |      |      |      |
|-------------|------|------|------|------|------|
| Year        | 1997 | 1998 | 1999 | 2000 | 2001 |
| Time Series | 87   | 90   | 92   | 98   | 105  |
|             | 2002 | 2003 | 2004 | 2005 |      |
|             | 93   | 100  | 110  | 125  |      |

OR

2) p) The rank of 10 students in a subject (A) and find the rank correlation coefficient for each of the three possible pairs.

|           |   |   |   |   |   |    |   |   |   |   |
|-----------|---|---|---|---|---|----|---|---|---|---|
| Rank in A | 1 | 3 | 4 | 2 | 5 | 10 | 8 | 6 | 7 | 9 |
| Rank in B | 3 | 5 | 1 | 2 | 6 | 10 | 4 | 9 | 7 | 8 |

q) Using least squares method, find the trend value. Also find trend for 2006.

|        |      |      |      |      |      |      |
|--------|------|------|------|------|------|------|
| Year   | 2000 | 2001 | 2002 | 2003 | 2004 | 2005 |
| Assets | 105  | 118  | 125  | 130  | 150  | 172  |

Q2] From the following data, find the regression equations and further estimate  $Y$  if  $X=16$  and  $X$  if  $Y=18$

|   |    |    |    |    |    |    |
|---|----|----|----|----|----|----|
| X | 3  | 4  | 6  | 10 | 12 | 13 |
| Y | 12 | 11 | 15 | 16 | 19 | 17 |

OR

Q2] A producer of product P has estimated the following distribution of demand.

|                       |      |      |      |      |      |
|-----------------------|------|------|------|------|------|
| No. of Units demanded | 0    | 1    | 2    | 3    | 4    |
| Probability.          | 0.15 | 0.25 | 0.30 | 0.20 | 0.10 |

Each unit of P cost him Rs 70 and he sells them at Rs 100 each. Any item left unsold is disposed at Rs 60 each. How many units of P should be produced so as to maximize his expected profit?

Q3] a) Calculate for the following data the index ( ) No. as given below:

- (i) Unweighted aggregative method
- (ii) Weighted aggregative method
- (iii) Unweighted average of price relatives
- (iv) Weighted average of price relatives

| Commodity | weight | Base Year | Current Year |
|-----------|--------|-----------|--------------|
| A         | 130    | 550       | 1345         |
| B         | 450    | 630       | 1250         |
| C         | 75     | 150       | 335          |
| D         | 225    | 450       | 778          |
| E         | 120    | 225       | 886          |

price in Rs.

b) For a bivariate distribution, the following ( ) results are obtained:

Mean value of  $x = 65$ , Mean value of  $y = 53$   
 Standard deviation of  $x = 4.7$ , Standard deviation of  $y = 5.2$ , Correlation coefficient,  $r = 0.78$

Find the two regression equations and hence obtain

- (i) the most probable value of  $y$  when  $x = 63$
- (ii) the most probable value of  $x$  when  $y = 50$

OR

Q3] p) From the following data calculate (i)  $I_L$  ( )  
 (ii)  $I_p$  (iii)  $I_f$

| Commodity | Base Year |          | Current Year |          |
|-----------|-----------|----------|--------------|----------|
|           | Price     | Quantity | Price        | Quantity |
| Rice      | 4         | 15       | 5            | 20       |
| Pulses    | 8         | 20       | 12           | 30       |
| Sugar     | 6         | 25       | 8            | 20       |
| D         | 6         | 3        | 8            | 4        |
| E         | 14        | 2        | 20           | 3        |

Q) A businessman has option to buy 3 plants, the choice depends on the expected sale volume. The payoff matrix is given as

| plant | Demand |          |      |
|-------|--------|----------|------|
|       | Low    | Moderate | High |
| $A_1$ | -5     | 5        | 20   |
| $A_2$ | 2      | 8        | 8    |
| $A_3$ | 4      | 5        | 5    |
| Prob  | 0.3    | 0.4      | 0.3  |

Construct a decision tree and recommend which plant should be bought.

## Section - II

Q. 4 a) Given  $f(x) = 3x^2 - 2$  for  $-5 \leq x < -2$   
 $= 4x - 1$  for  $-1 \leq x \leq 1$   
 $= x^3 + x - 4$  for  $2 \leq x \leq 6$

find  $f(0)$ ,  $f(-3)$  &  $f(4.5)$

b) A person borrowed totally RS. 160,000 from two known people. For one loan he paid 18% p.a. and for the second loan, he paid ~~18%~~ 25% p.a. After one year, he paid RS. 31,600 as Simple Interest. How much money did he borrow at each rate.

OR.

4 p] Examine the following function for maxima & minima

$$f(x) = 10x^3 - 15x^2 + 10$$

q] A cottage industry of toys has 29 workers. The Fixed Cost turns out to be RS. 30 per worker daily. The cost of producing a unit toy is RS. 2.07.

i) If each toy is sold for RS. 6, find the no. of toys that should be produced and sold to ensure no loss.

ii) If to promote sale, price is reduced by 50 paise per toy, what would be the Break-Even point

5 a) Find  $\frac{dy}{dx}$ , where

i)  $y = \frac{5x+4}{4x+5}$

ii)  $y = (x^2 - 3x + 5)(e^x + 1)$

b) A loan of Rs. 50,000 is to be returned in 3 equal monthly instalments, the rate of Interest being 2% per month.

i) Calculate the EMI using reducing balance method.

ii) Find Interest & principle repayment Components of the EMI for each month.

OR.

5 P] On what sum of money will the difference between the Compound Interest and the Simple Interest for two years at 4% p.a. be Rs. 56?

Q] The demand for a commodity when its price is  $x$  is given by

$$y = \frac{2x+5}{3x-4}$$

Find the elasticity of demand when the price is 5 units.